



Imaging with entangled photons

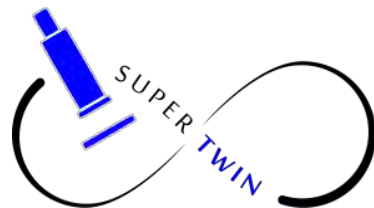
L. Gasparini¹, M. Perenzoni¹, H. Xu¹, L. Parmesan¹, M. Moreno Garcia¹,
D. Stoppa⁴, B. Bessire², M. Unternährer², A. Stefanov²,
V.Mitev³ and D.L. Boiko³

¹*Fondazione Bruno Kessler, Italy*

²*Institute of Applied Physics, University of Bern, Switzerland*

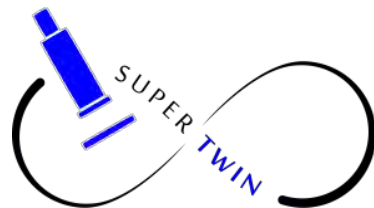
³*Centre Suisse d'Électronique et de Microtechnique CSEM, Switzerland*

⁴*now at AMS-Heptagon, Switzerland;*



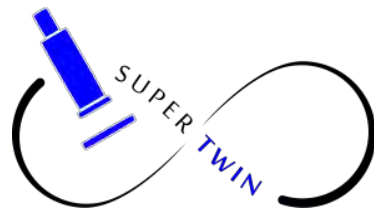
Outline

- Motivation
- Requirements for imaging with entangled photons
- SuperEllen imager design and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



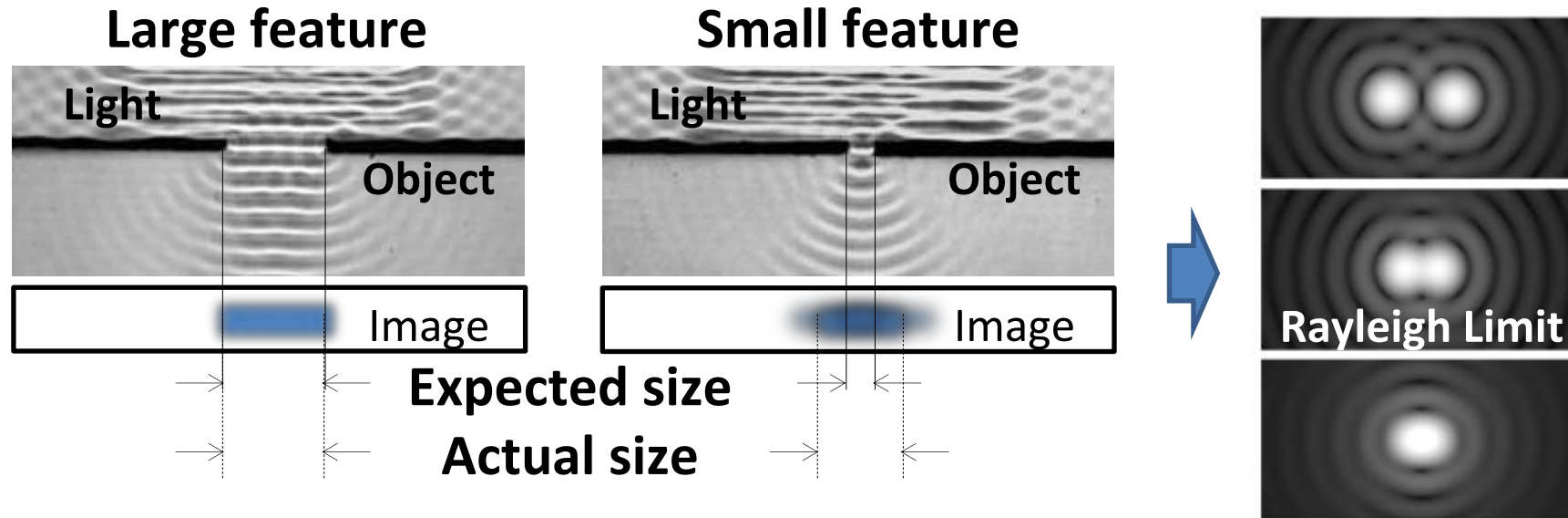
Outline

- **Motivation**
- Requirements for imaging with entangled photons
- SuperEllen imager design and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



Conventional Optical Microscopy Limits

- Light as a wave: **diffraction** limits resolution



- Limit is the wavelength λ
 - With visible light: $\lambda/2$, about 250nm
 - Cells: $\approx 10\mu\text{m}$ 😊 Viruses: $\approx 100\text{nm}$ ☹️



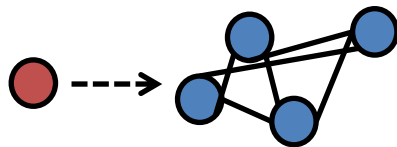
Beyond Rayleigh: SUPERTWIN Concept

- Light as a particle
- N entangled photons \Rightarrow de Broglie wavelength λ/N

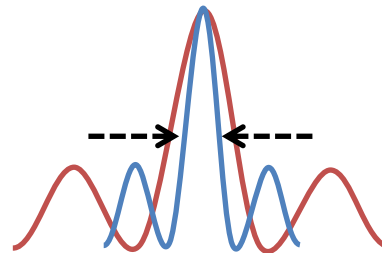
N measurements with N detectors give N times improvement

SUPERTWIN

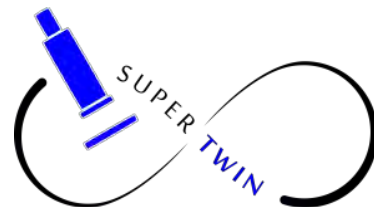
N^{th} entanglement



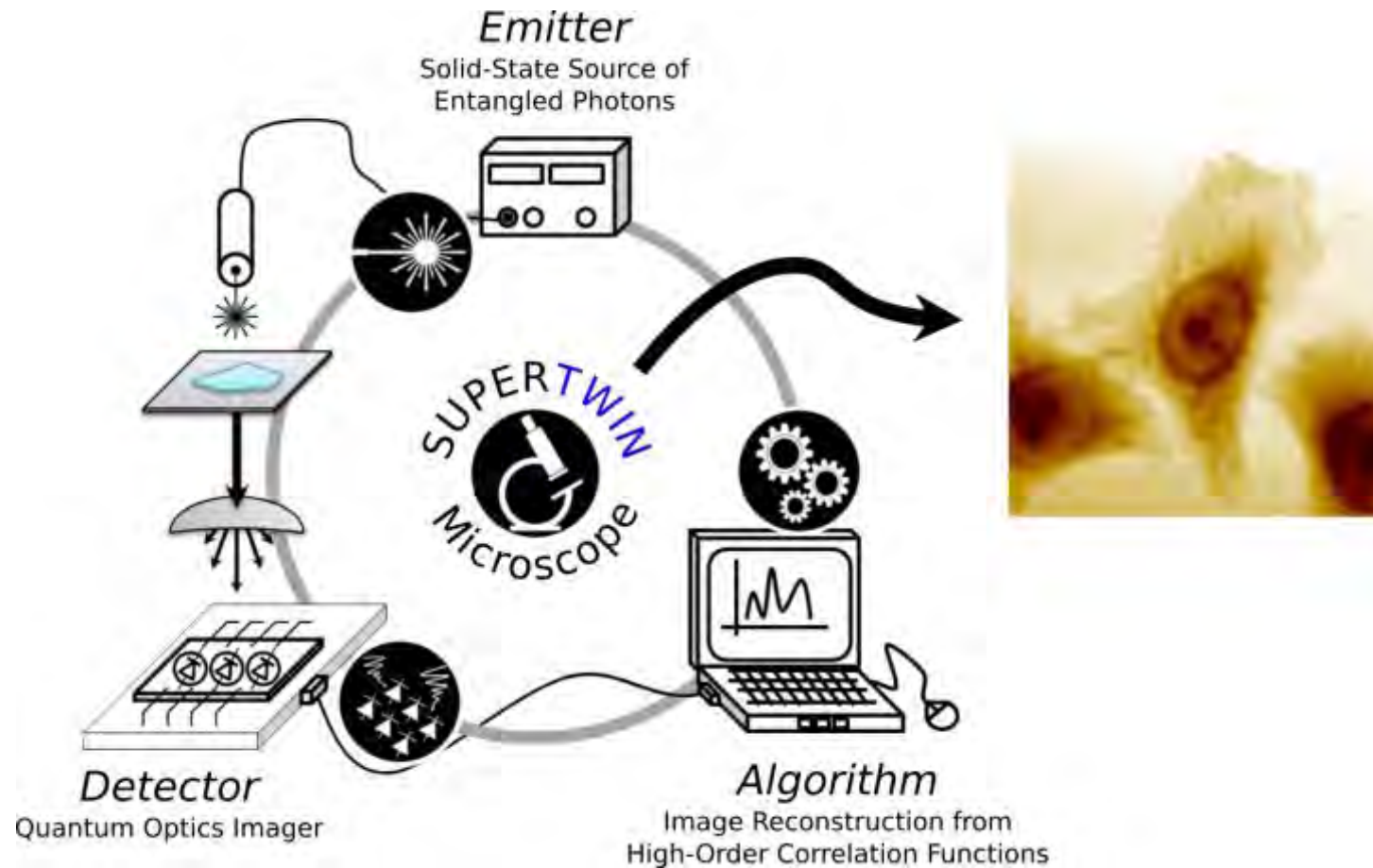
$:N$ diffraction



$\times N$ resolution



SUPERTWIN Concept & Goal

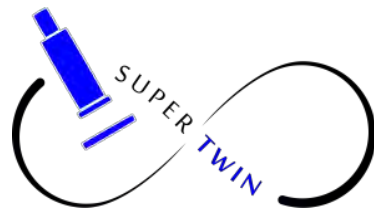


Advanced All-Solid State Optical Microscope Imaging Beyond the Rayleigh Limit



Outline

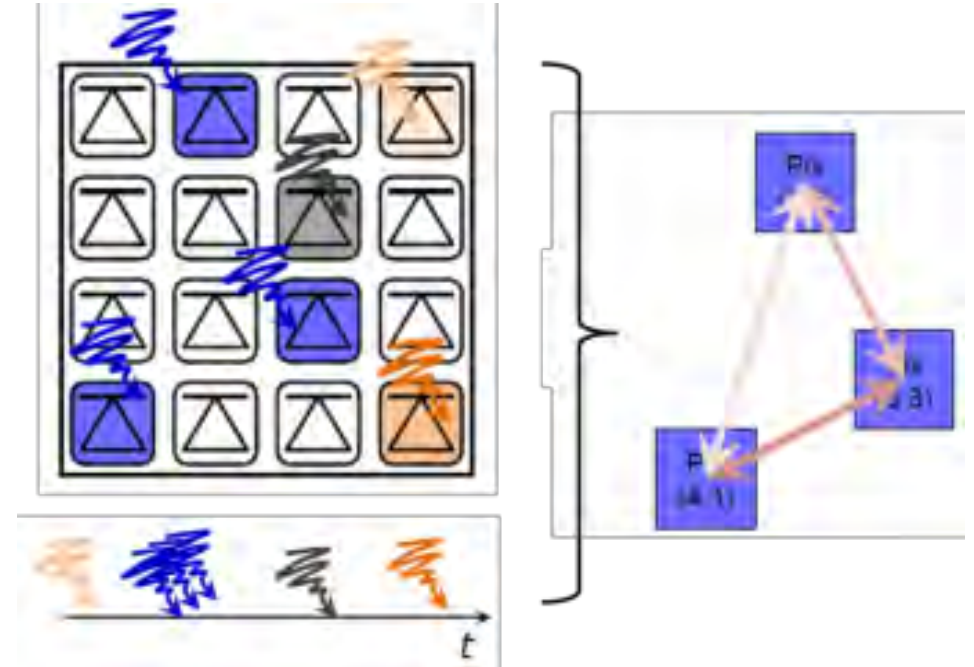
- Motivation
- **Requirements for imaging with entangled photons**
- SuperEllen imager design and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



CMOS Single-Photon Imager

- Scattered entangled photons
 - Spread in space (non-local)
 - Simultaneous in time
- Single photon imager
 - **Position + Time**

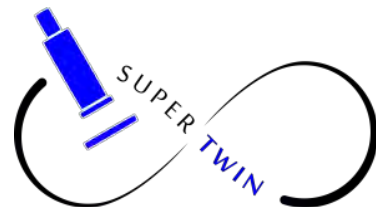
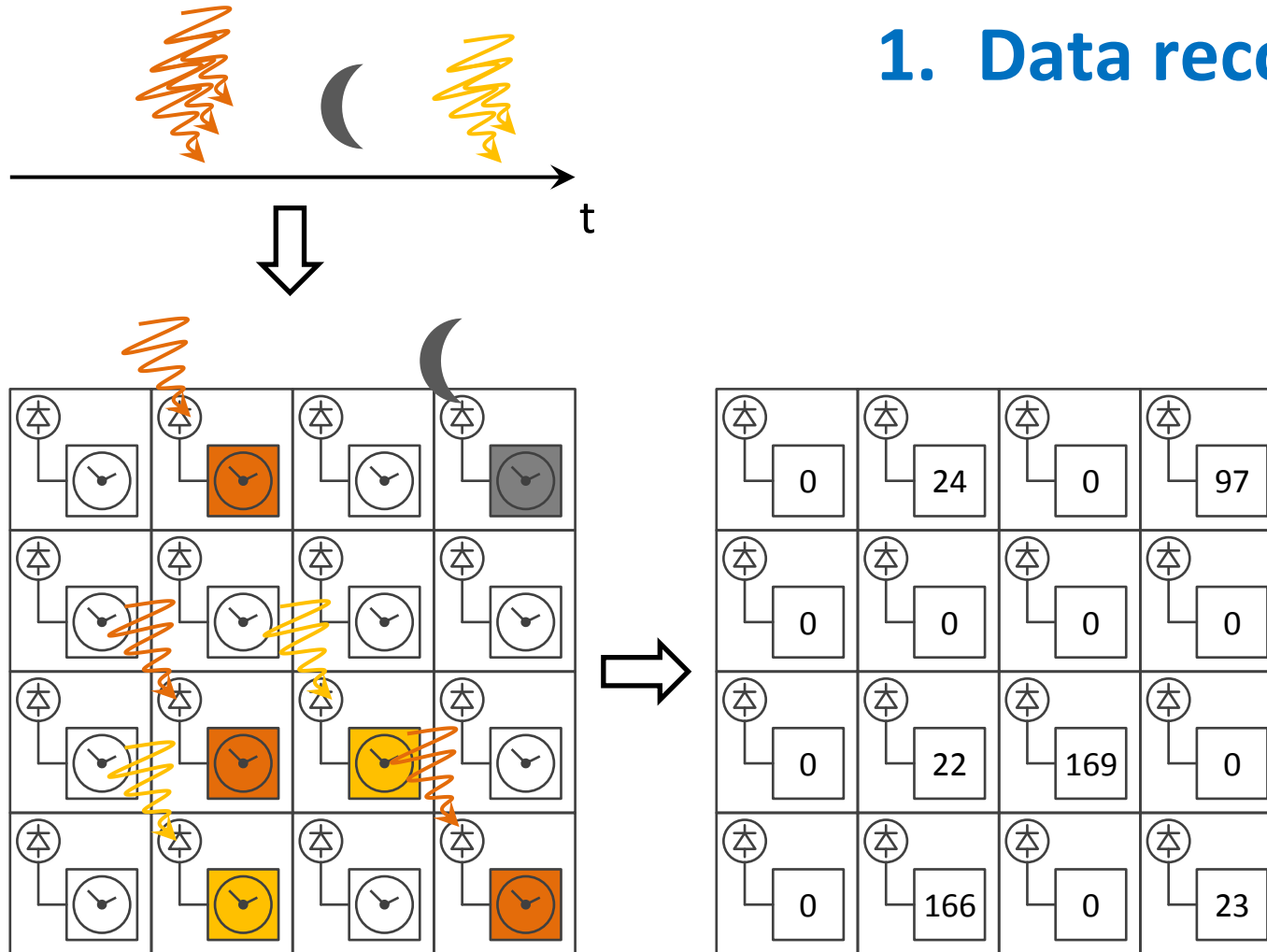
$$(x, y) + \text{⌚}$$



Goal: extraction of N^{th} order correlation function $G^{(N)}$

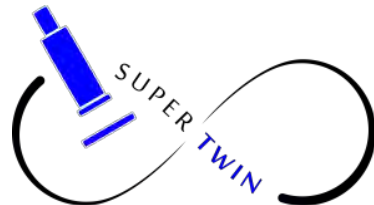
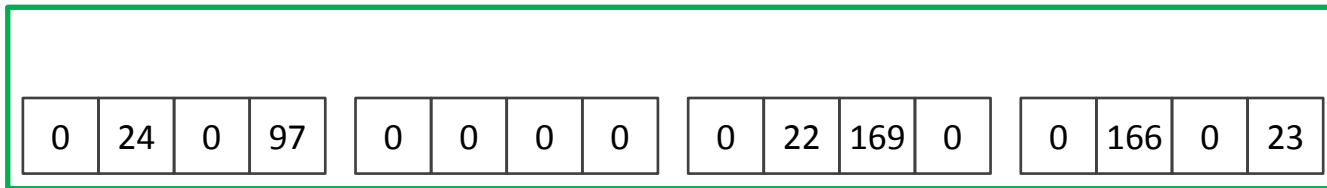
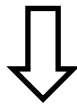
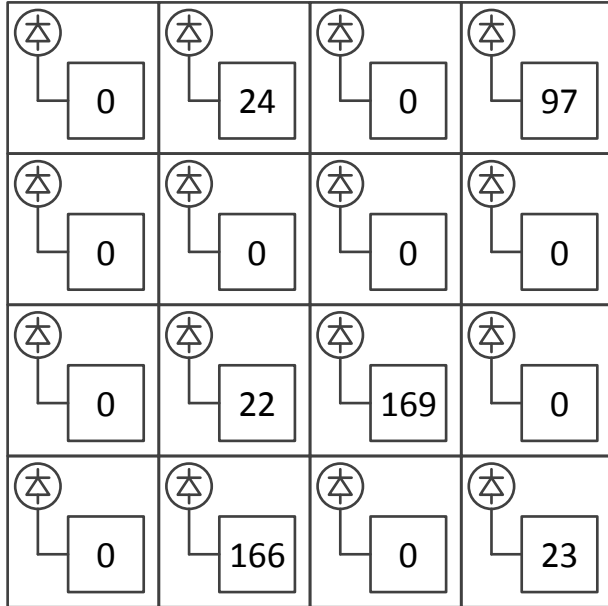
Data processing flow

1. Data recording

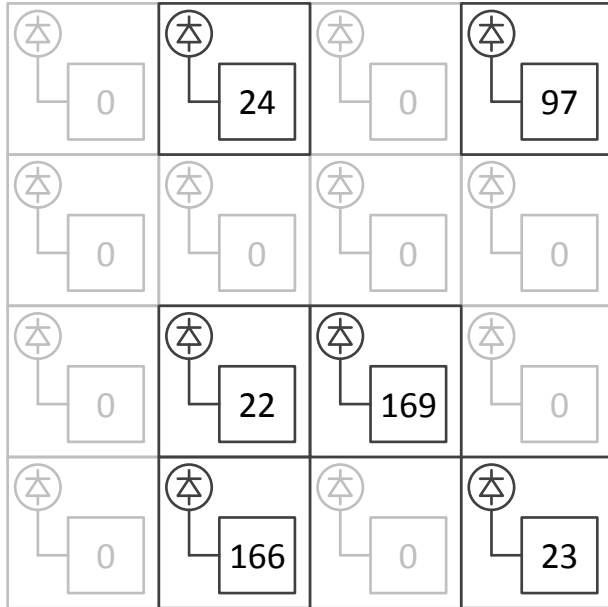


Data processing flow

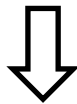
1. Data recording
2. Readout



Data processing flow



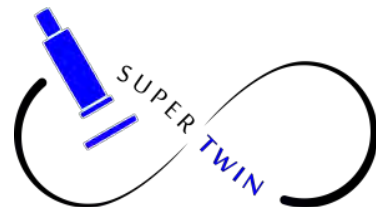
1. Data recording
2. Readout
3. **Compression**



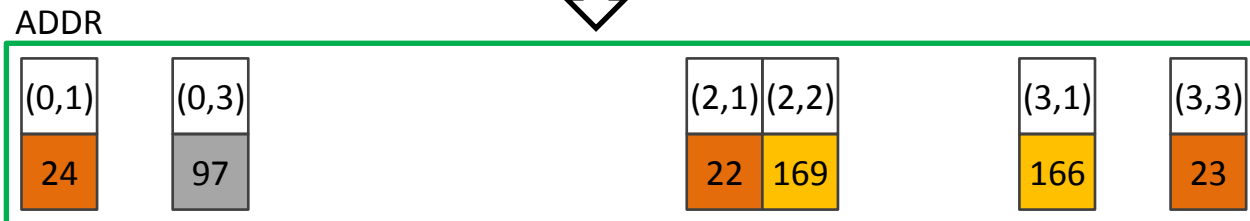
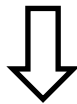
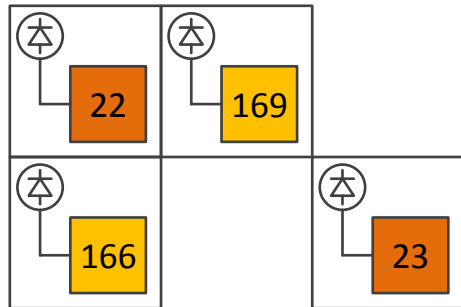
ADDR



TDC CODE

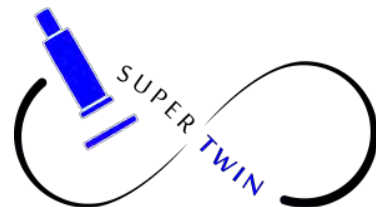


Data processing flow

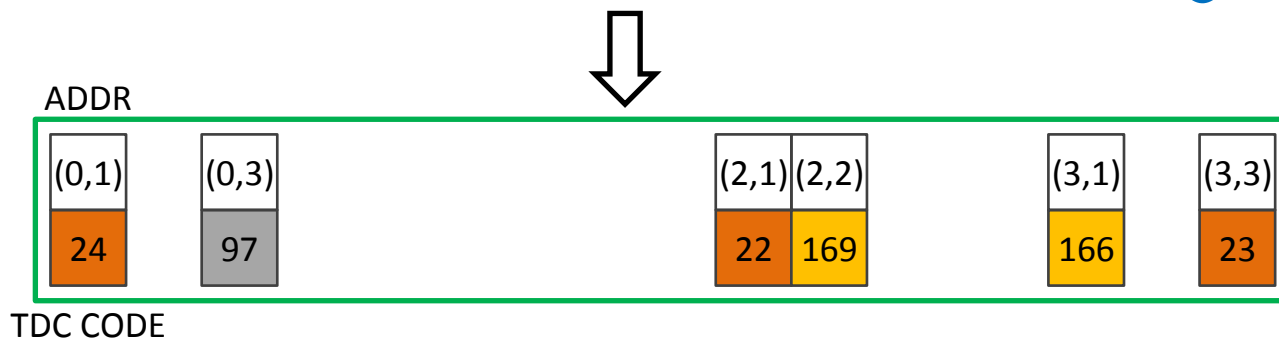


TDC CODE

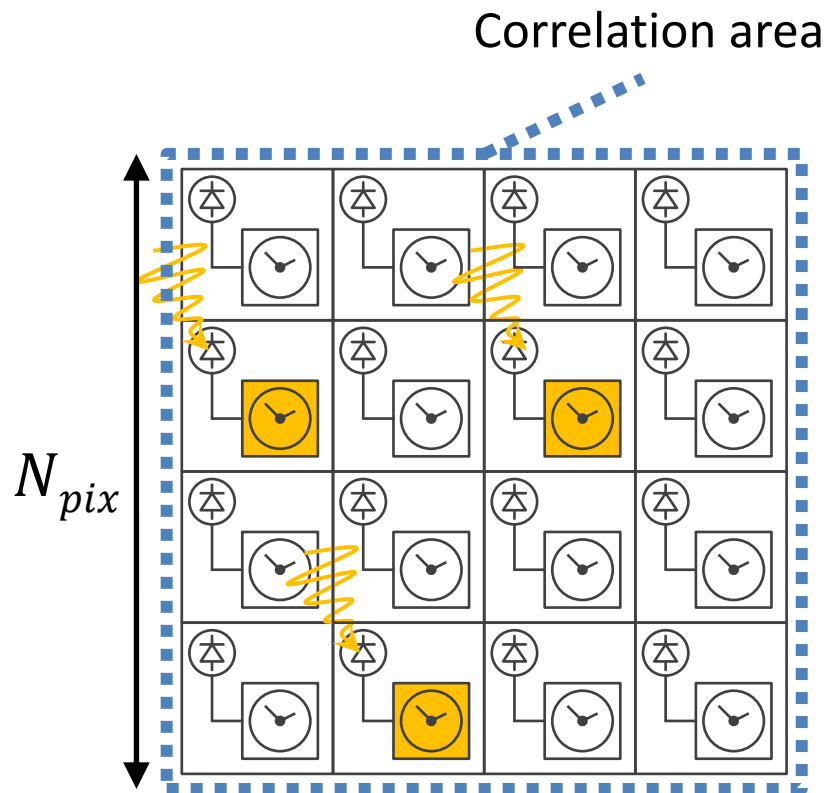
1. Data recording
2. Readout
3. Compression
4. Coincidence detection



Data processing flow



Memory requirements – Full area correlations

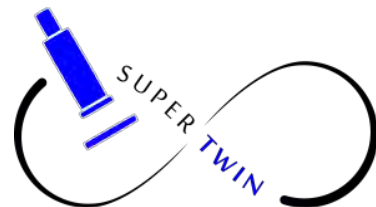


- $G^{(k)} \rightarrow k$ -dimensional space

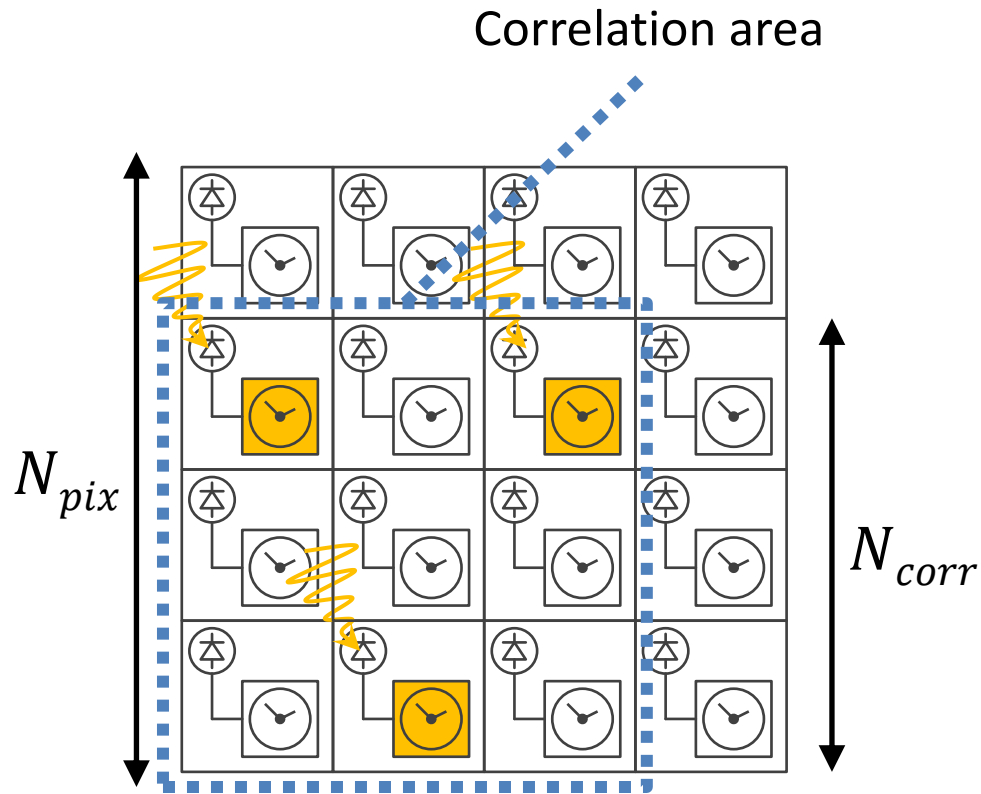
- Histogram size = $\frac{N_{pix}!}{k!(N_{pix}-k)!}$

Hypothesis: 2G memory

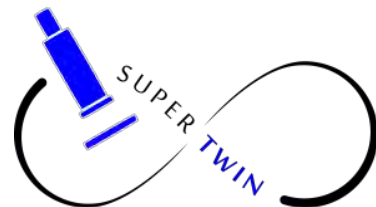
- Feasible up to:
 - 32×32 array $\rightarrow G^{(3)}$
 - 256×256 array $\rightarrow G^{(2)}$



Memory requirements – Reduced area correlations

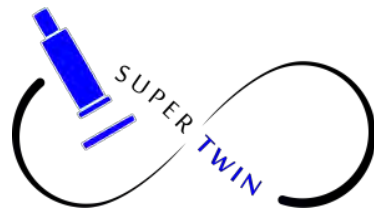


- $G^{(k)} \rightarrow k$ -dimensional space
- Histogram size = $\frac{N_{pix}!}{k!(N_{pix}-k)!}$
- Feasible up to:
 - $G^{(5)}$ with $N_{corr} = 16$
 - $G^{(4)}$ with $N_{corr} = 24$
 - $G^{(3)}$ with $N_{corr} = 48$
 - $G^{(2)}$ with $N_{corr} = 256$



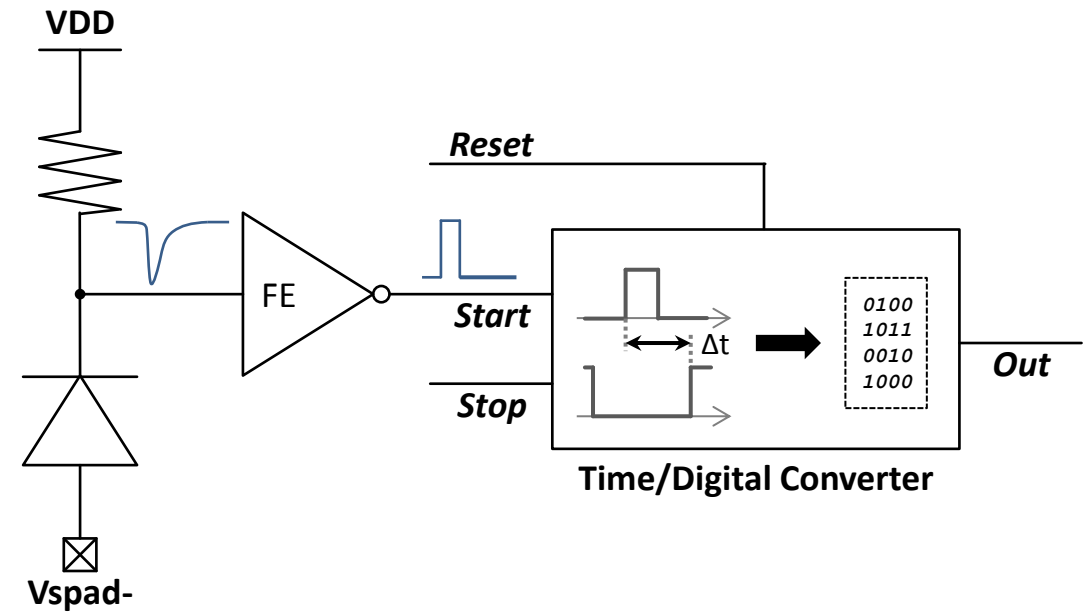
Outline

- Motivation
- Requirements for imaging with entangled photons
- SuperEllen imager design and characterization
- $G^{(2)}$ correlations in SPDC –produced bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



SuperEllen SPAD Imager

- Previous SPAD+TDC designs:
 - Large pixel $>50\mu\text{m}$
 - Small FF $< 3\%$
 - Huge amount of data
- Pixel array based on TDC, target:
 - Low pitch
 - High FF
 - Fast readout



SuperEllen SPAD Imager

CMOS 150nm tech

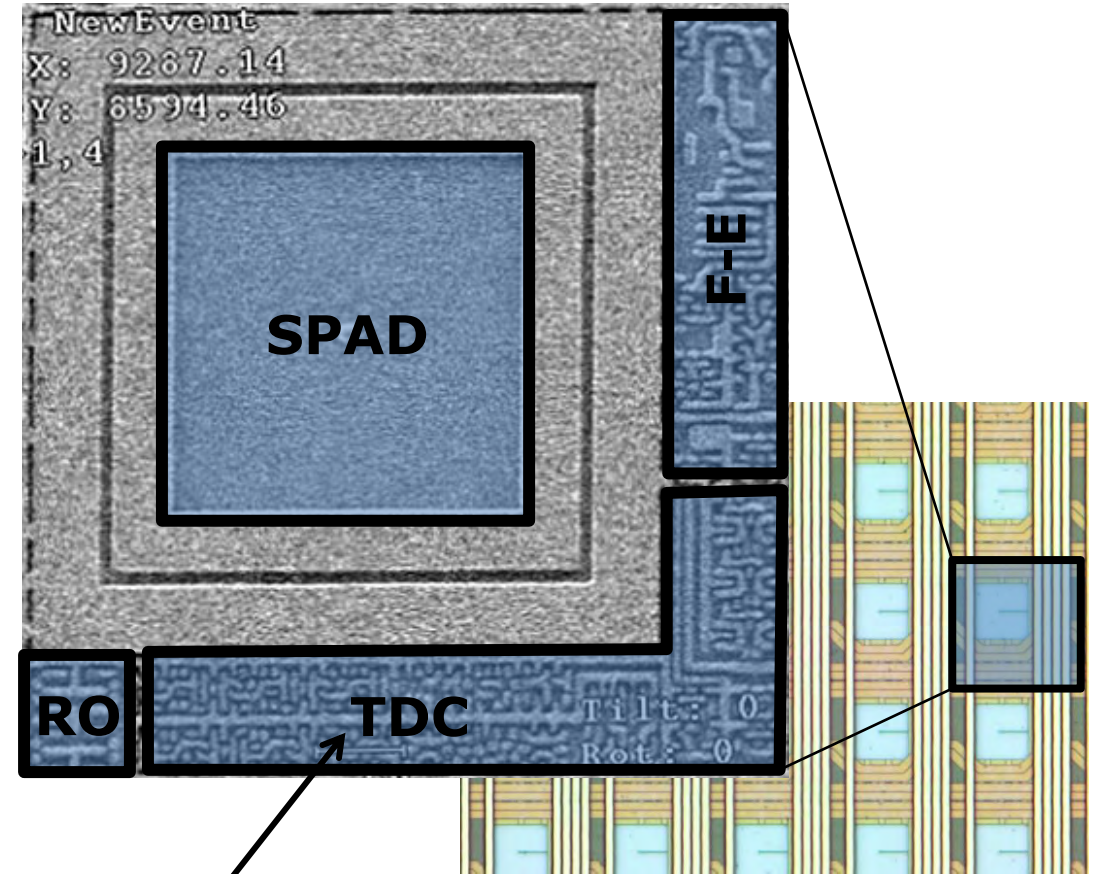
SPAD: p+/nwell

TDC: 8b, 205ps

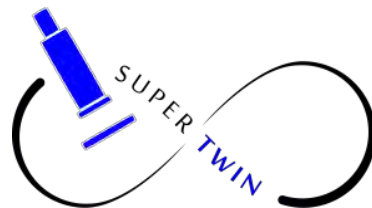
R-O: row/frame skip

- **Pixel array based on TDC, result:**

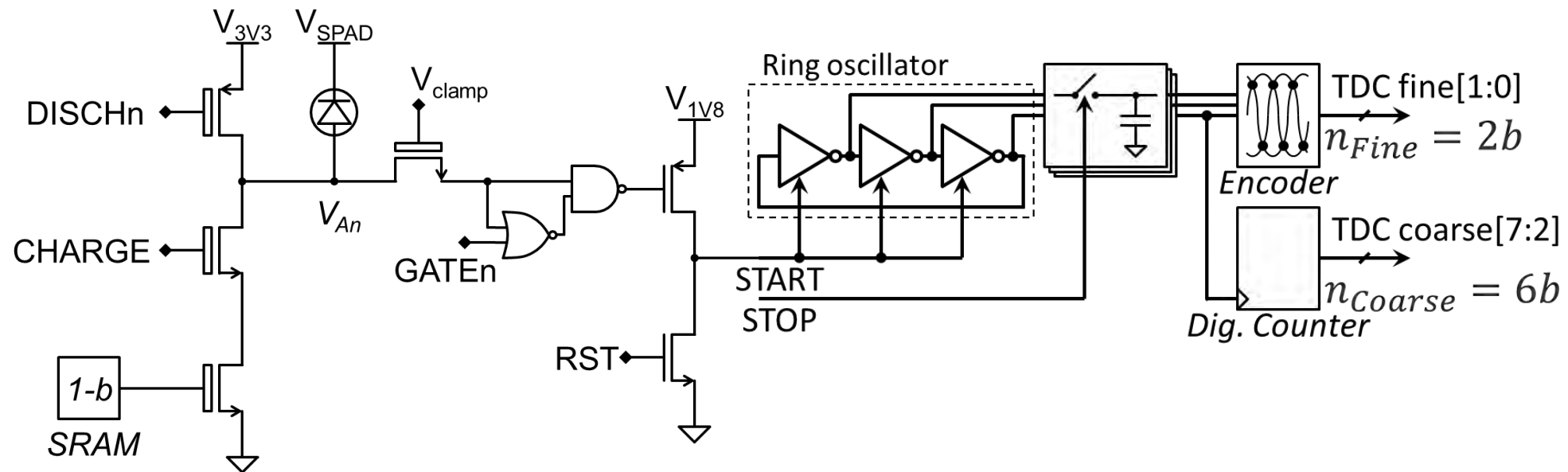
- **Low pitch** **44.6 μ m**
- **High FF** **19.5%**
- **Fast readout** **800kfps**



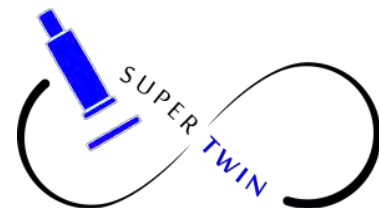
$\approx 20T/bit$
 $\approx 400\mu m^2$



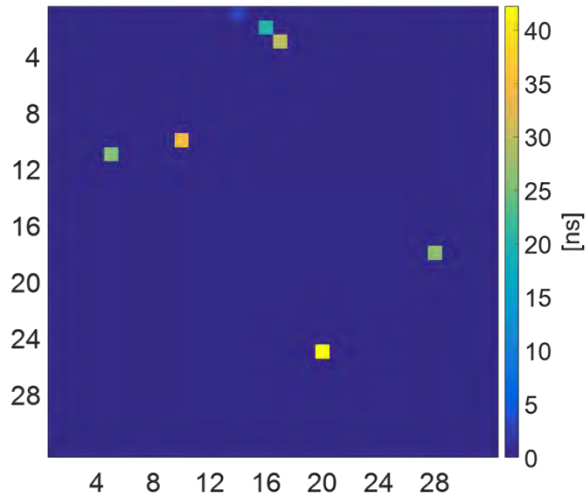
Pixel and TDC Concept



- Synchronous SPAD precharge with disable SRAM
- Edge-sensitive START and gated operation
- Ring-oscillator based TDC with 2b interpolation

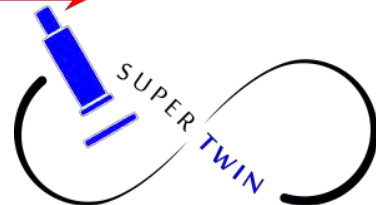
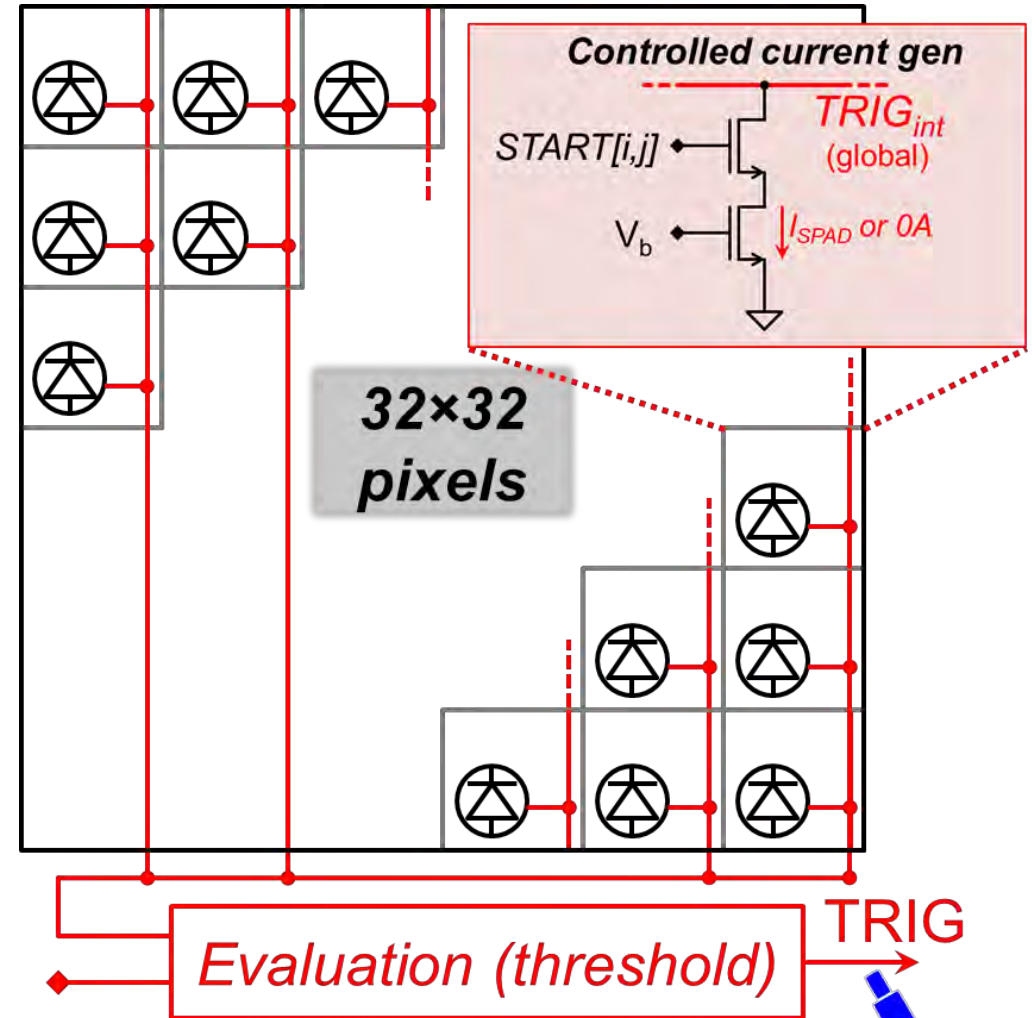


Imager Readout Concept

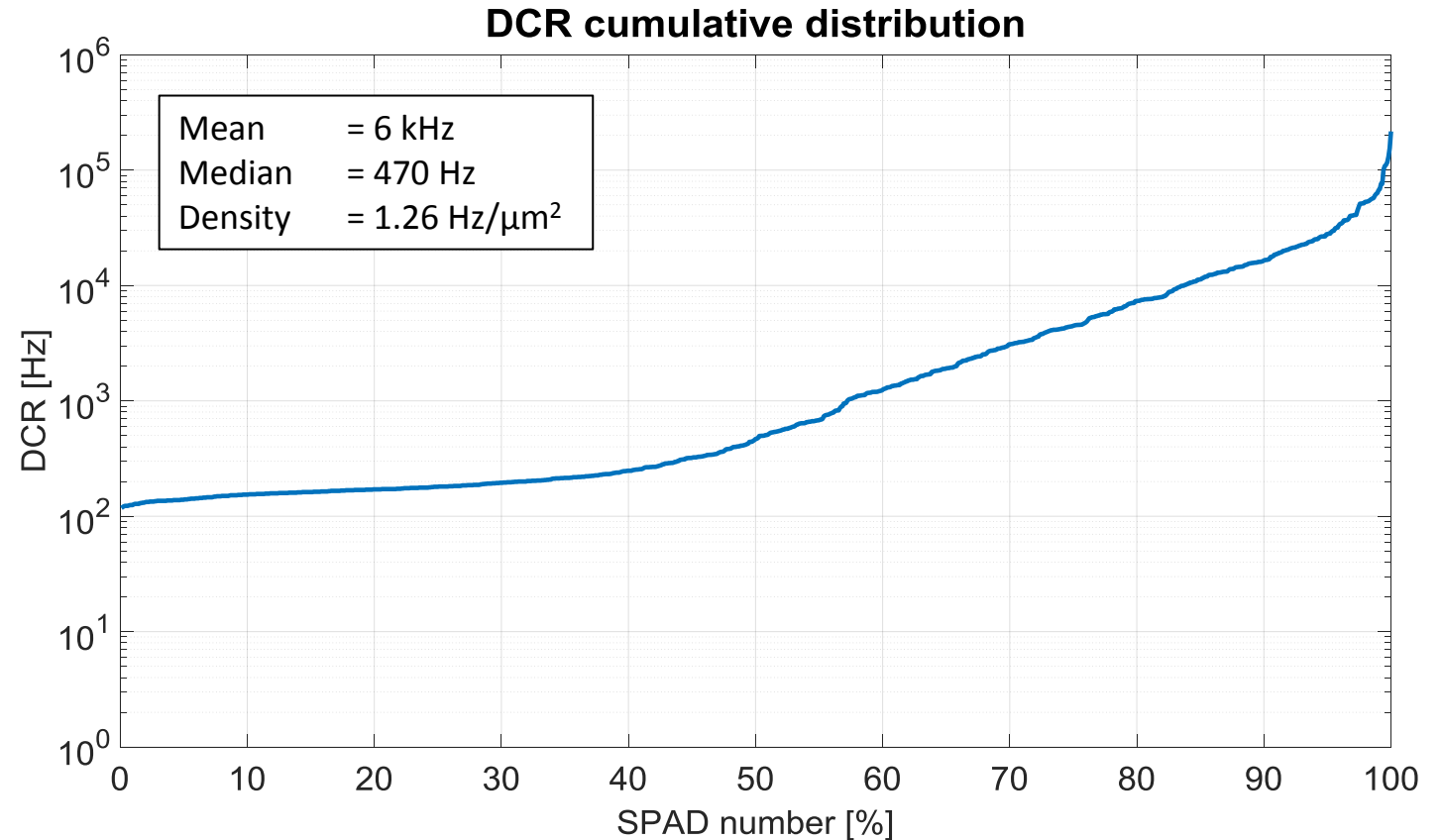
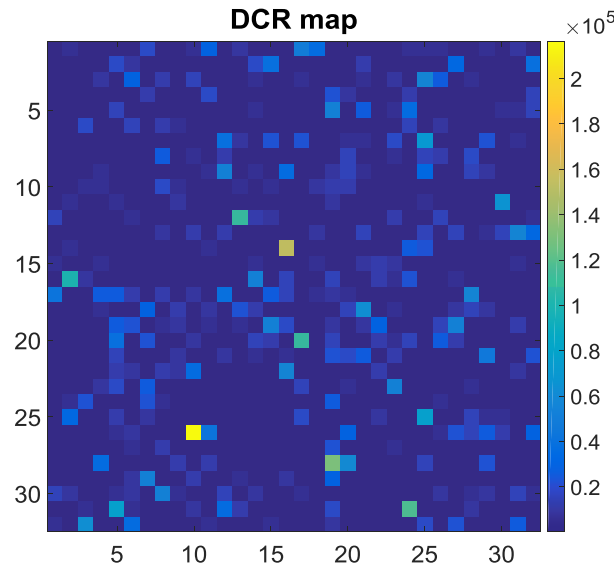


- Row-wise “empty row detection”
- Current-based global threshold

➔ **x10 gain in acq duty-cycle**



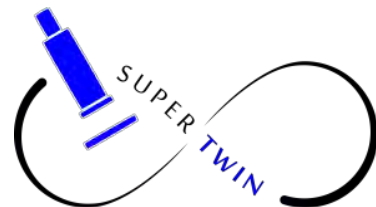
SPAD Dark Count Rate (DCR)



- SPAD

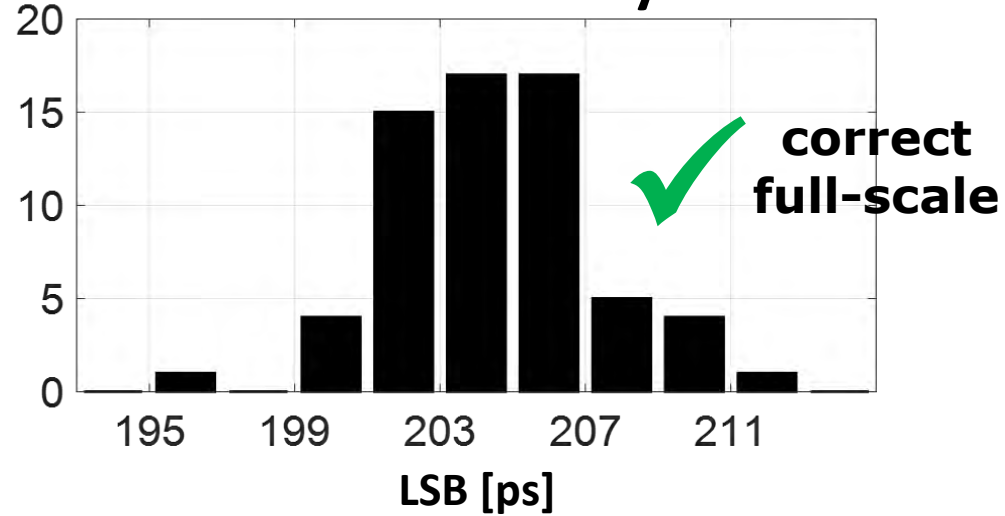
- 20 μm square w/rounded corners

- p+/nwell (no sharing) ➔ **Minimize xtalk**

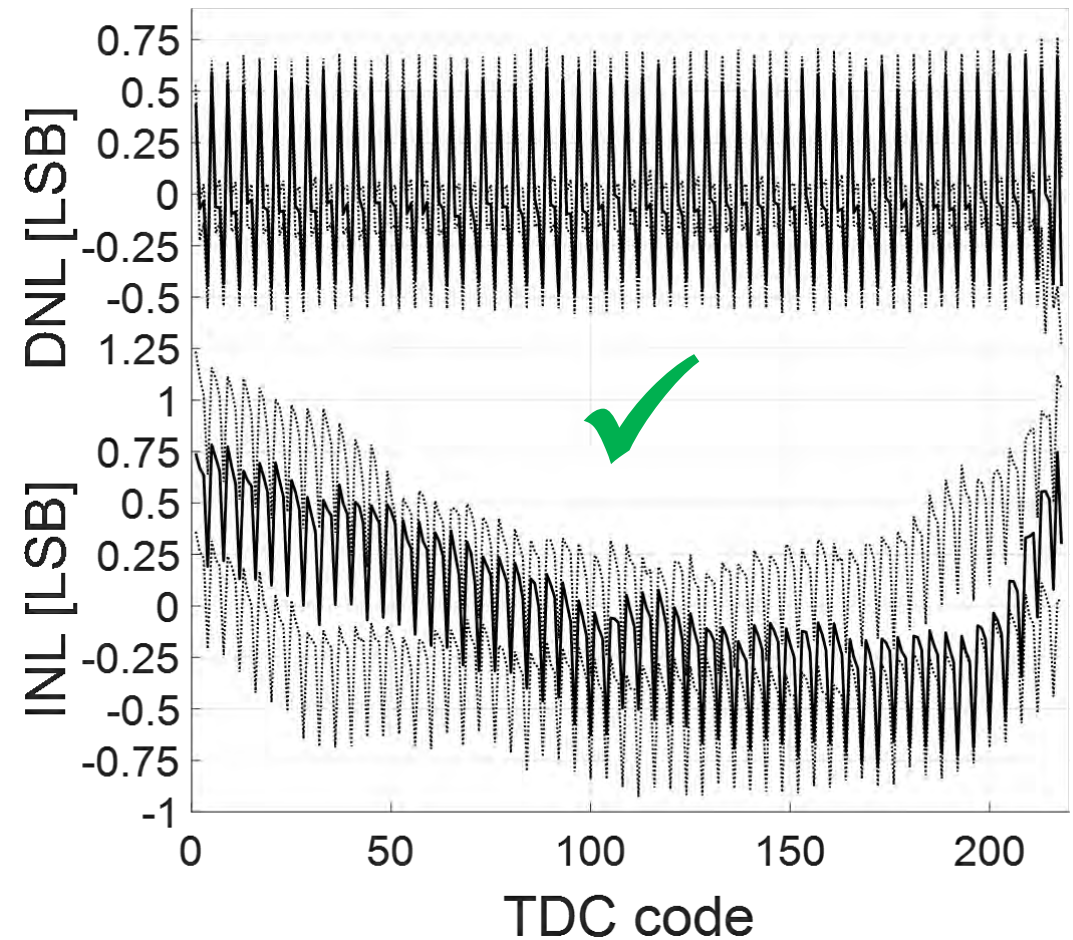
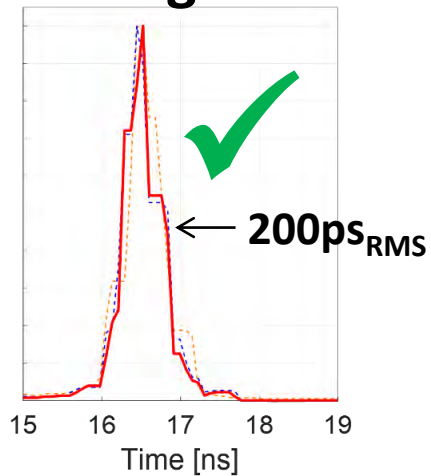


Pixel/Array Timing Performance

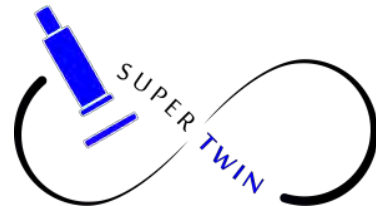
TDC Uniformity



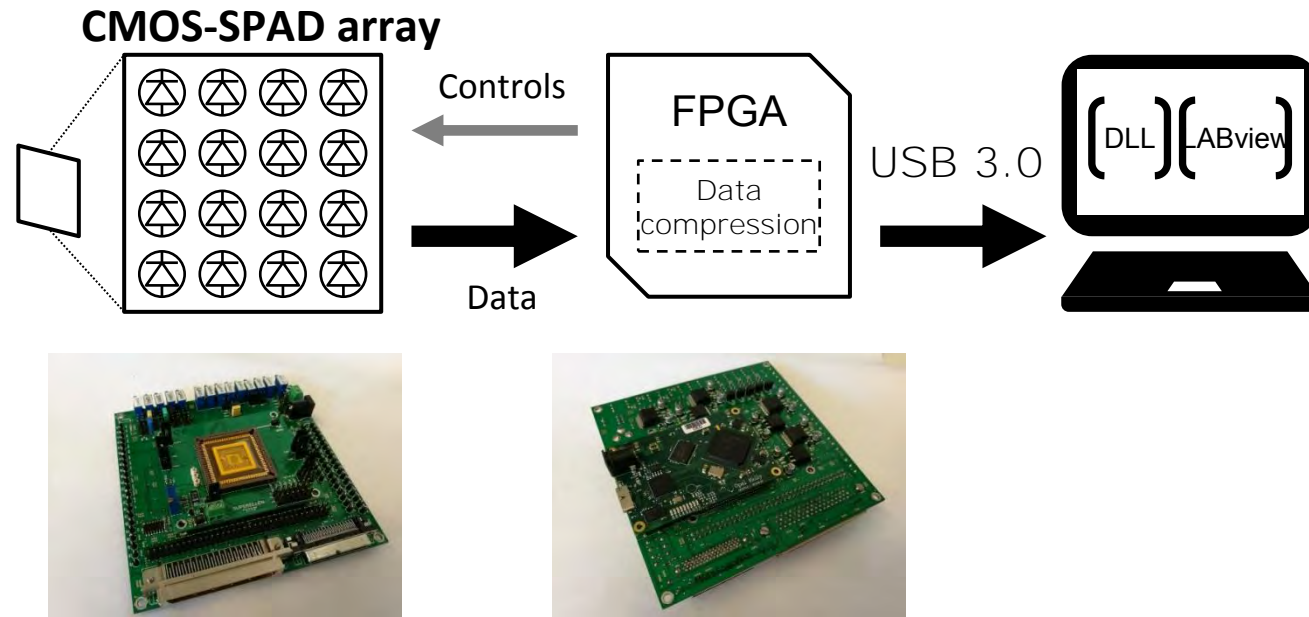
Timing Jitter



Goal: detect non-local correlations



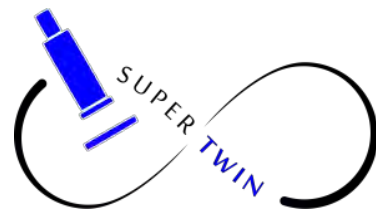
Demonstrator of Quantum Imager



- Frame rate in the **80-500 kfps** range
- **Real-time data compression** exploiting sparsity of data
 - Raw frame = 1kB; compressed frame < 30B (typ) → **3% compression ratio**
 - Address assignment performed by the FPGA
- **Software-based** calculation of correlation functions $G^{(N)}$

Outline

- Motivation
- Requirements for imaging with entangled photons
- SuperEllen fabrication and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



Generation of bi-photons

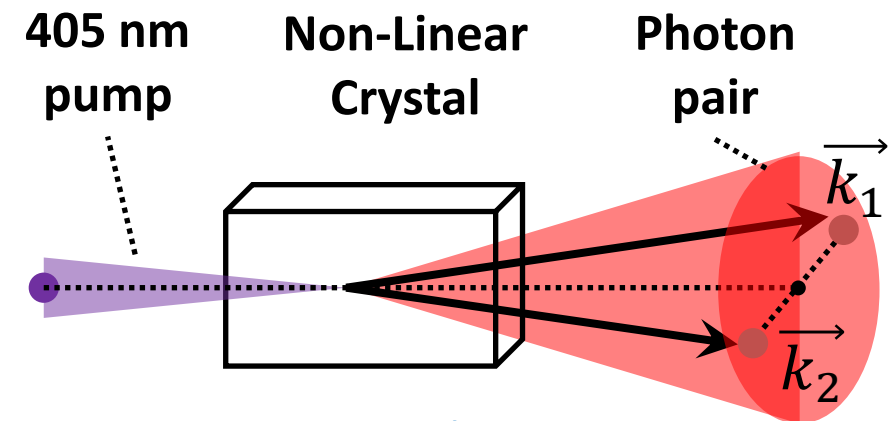
- PPKTP: phase matching in type-0 SPDC

- Energy conservation:

- 1 ph @405 nm \rightarrow 2 ph @~810 nm

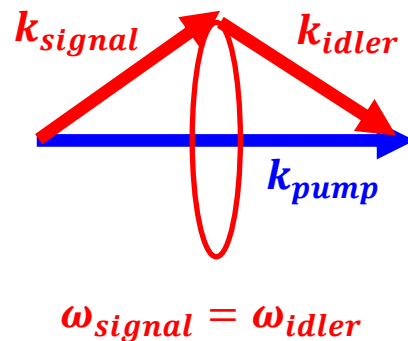
- Momentum conservation

- Different patterns wrt temperature (with T_c critical temperature)



Non-collinear, degenerate:

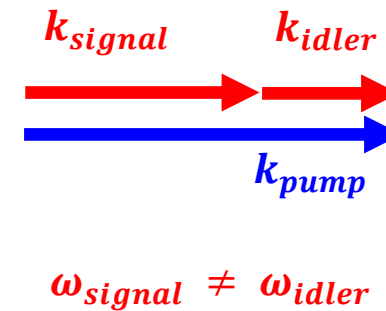
Wavevectors of bi-photons on a cone, anticorrelated



$T < T_c$

Collinear, non-degenerate:

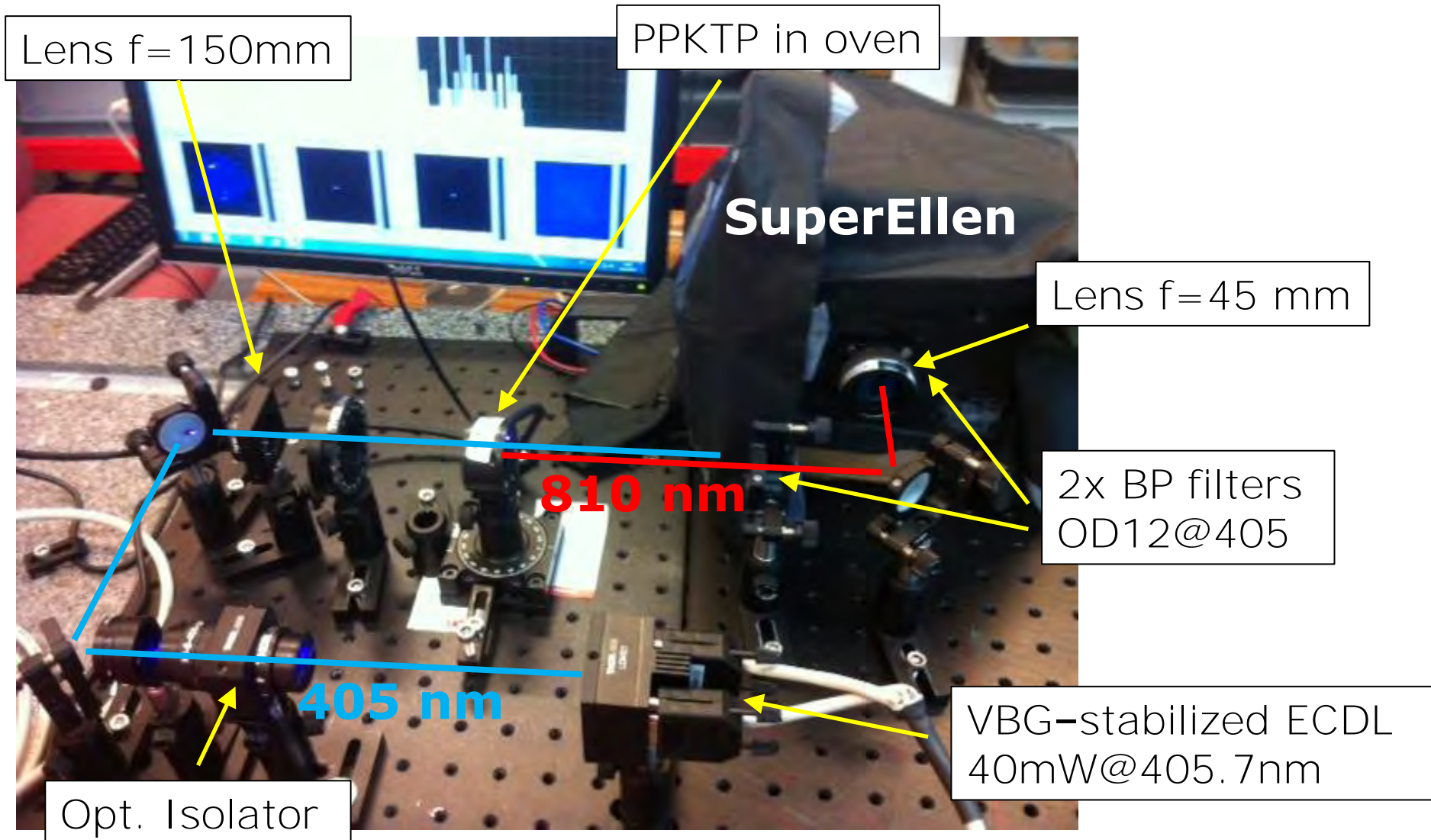
Transversal wavevectors of bi-photons, correlated



$T > T_c$

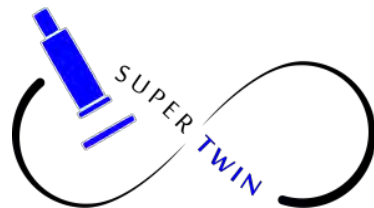
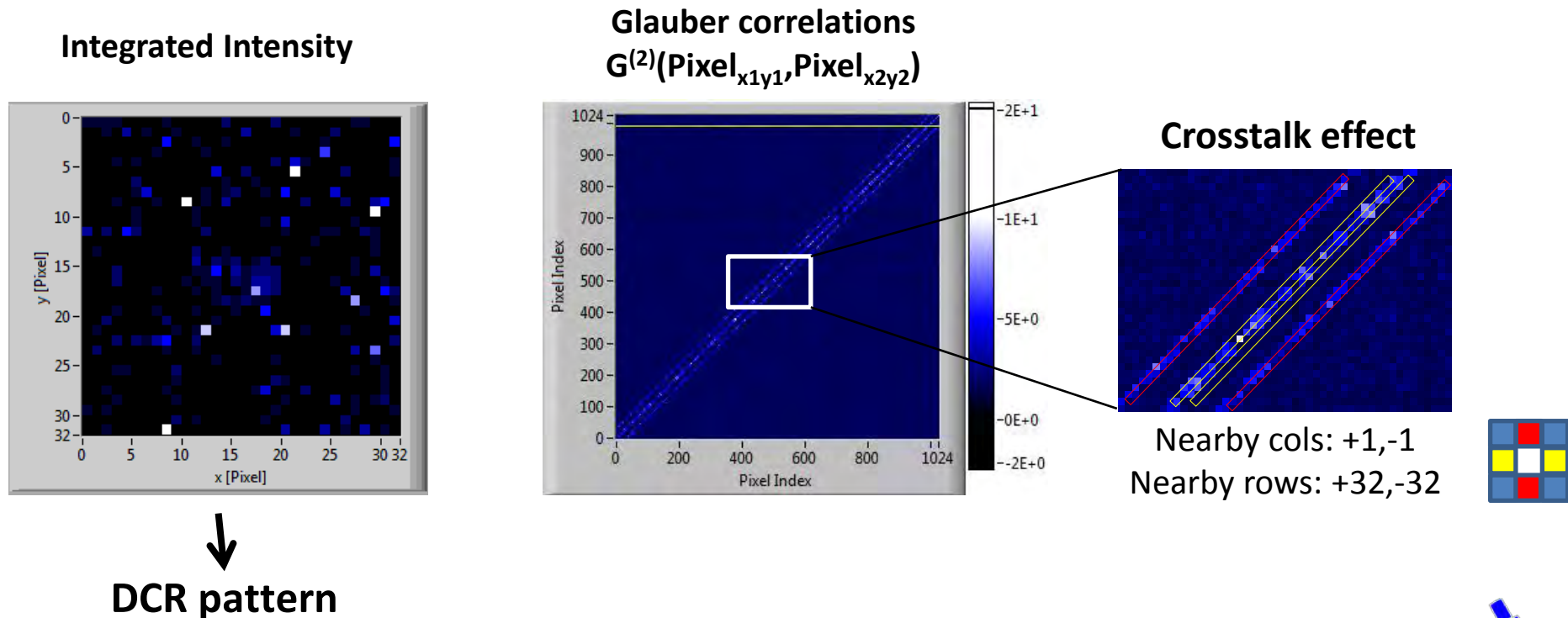


SPDC Laboratory Setup



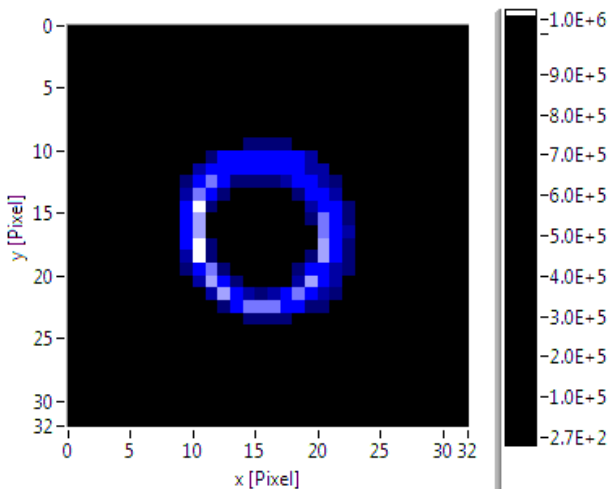
Effects of DCR and Crosstalk – Source OFF

- Intensity: just accumulation of hits
- $G^{(2)}$: linearized index on x and y axis of coincidences

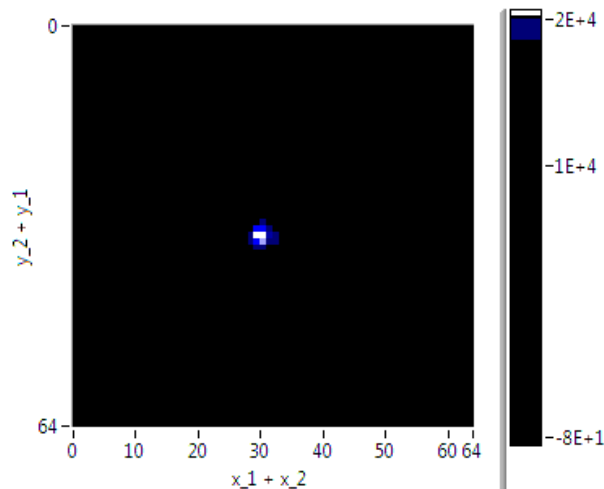


Anticorrelated Bi-photons ($T < T_c$)

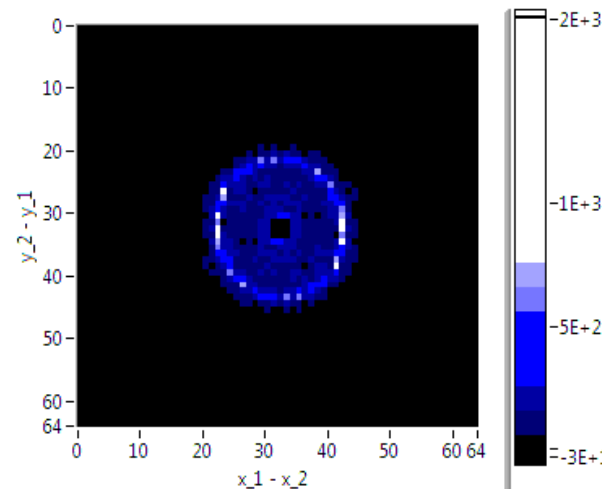
Integrated Intensity



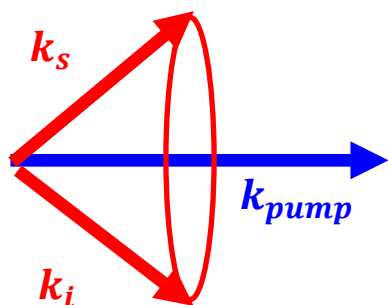
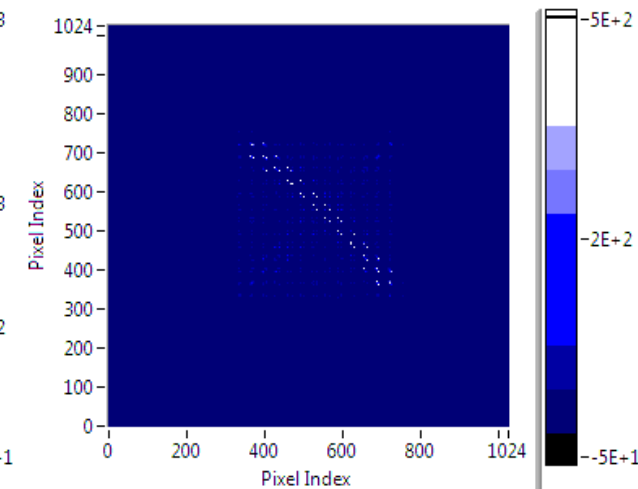
Integrated anticorrelations
 $\int G^{(2)}(\Delta+k, \Delta-k) dk$



Integrated correlations
 $\int G^{(2)}(\Delta+k, \Delta+k) d\Delta$



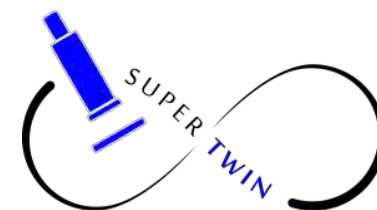
Glauber correlations
 $G^{(2)}(\text{Pixel}_{x_1y_1}, \text{Pixel}_{x_2y_2})$



↓
Narrow correlation range around central position of spot

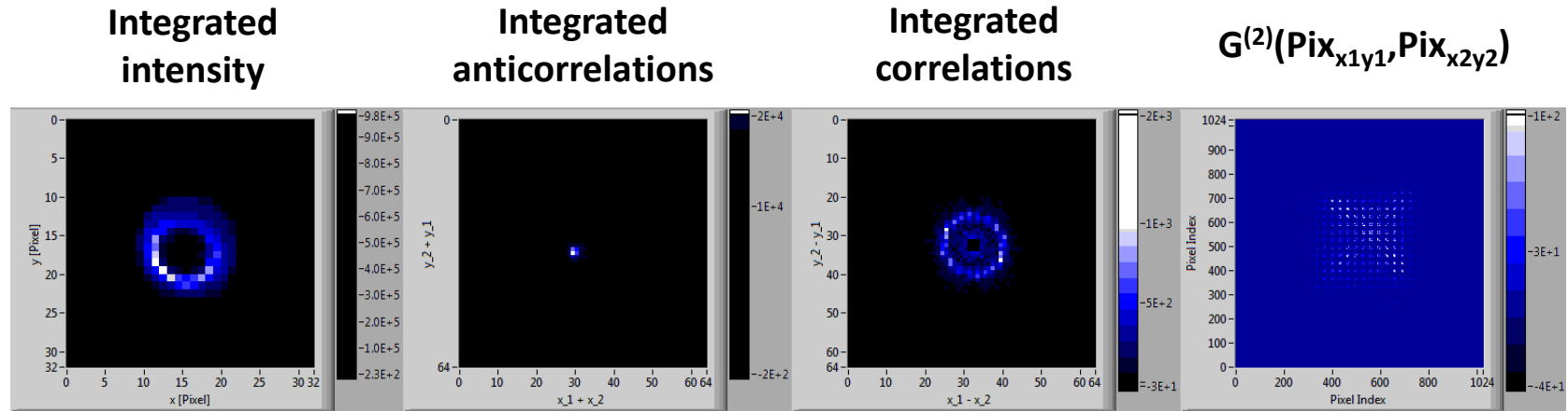
↓
Reproduces ring of “constant distance”, confirming correlations

↓
Anti-diagonal attests for anticorrelations

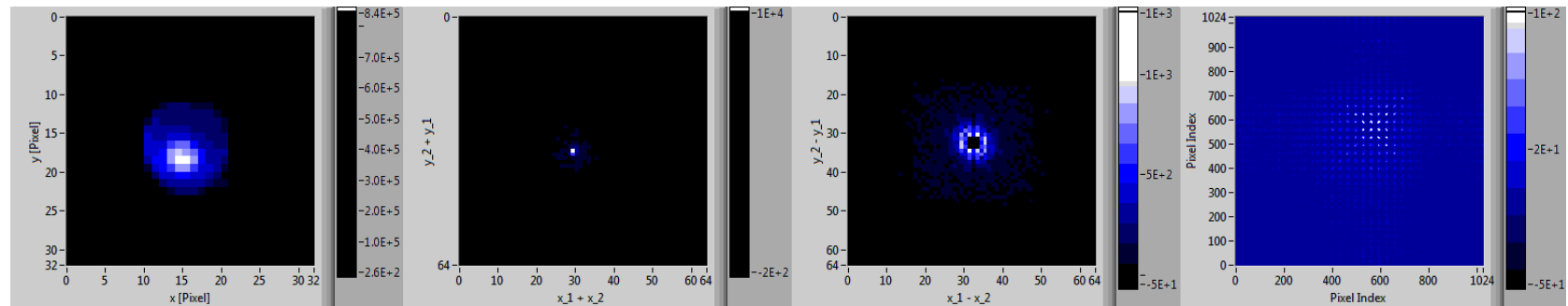


Matching Theory: SPDC Generation vs. Temperature

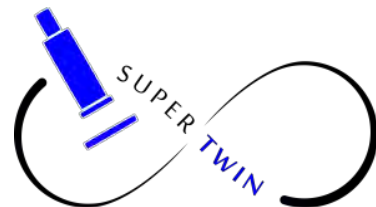
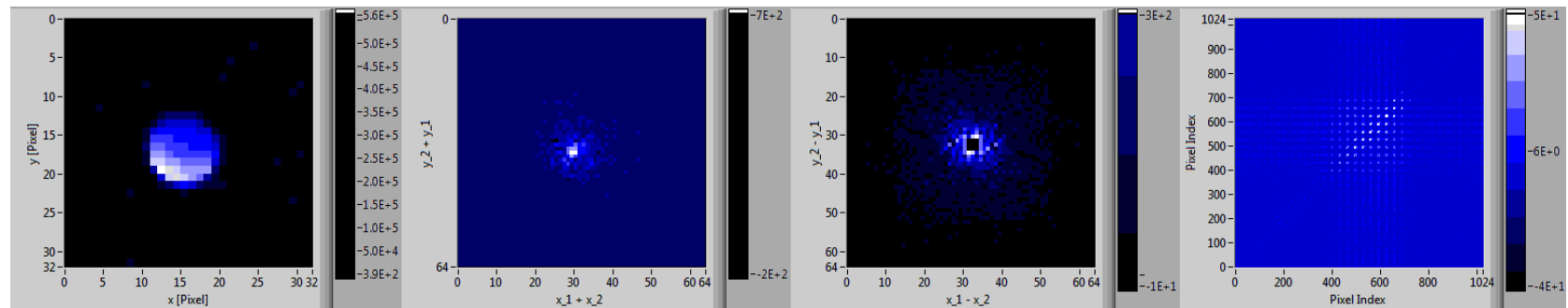
$52.5^{\circ}\text{C} < T_c$
Anticorrelations



$55.0^{\circ}\text{C} = T_c$
Degeneracy

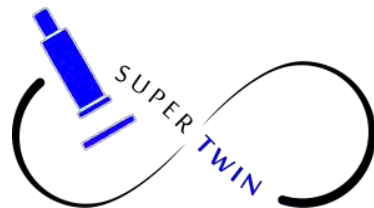


$57.5^{\circ}\text{C} > T_c$
Co-propagating bi-photons



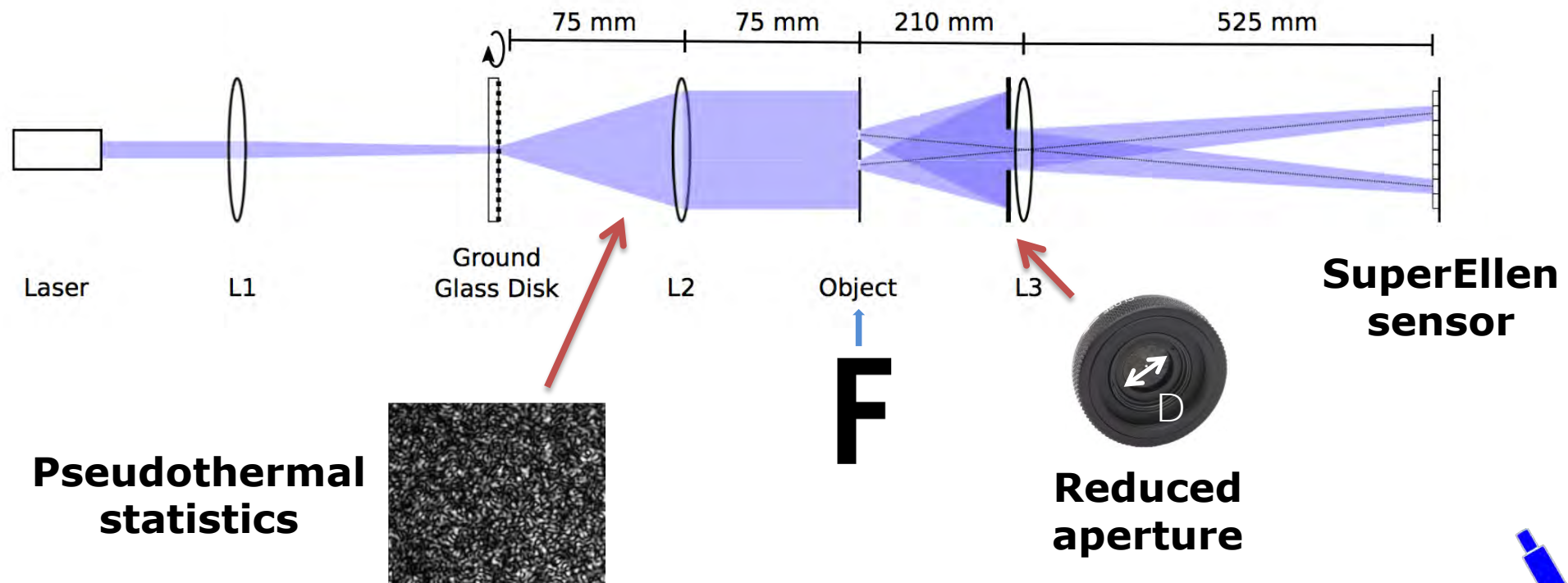
Outline

- Motivation
- Requirements for imaging with entangled photons
- SuperEllen fabrication and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook

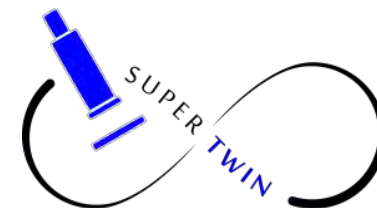
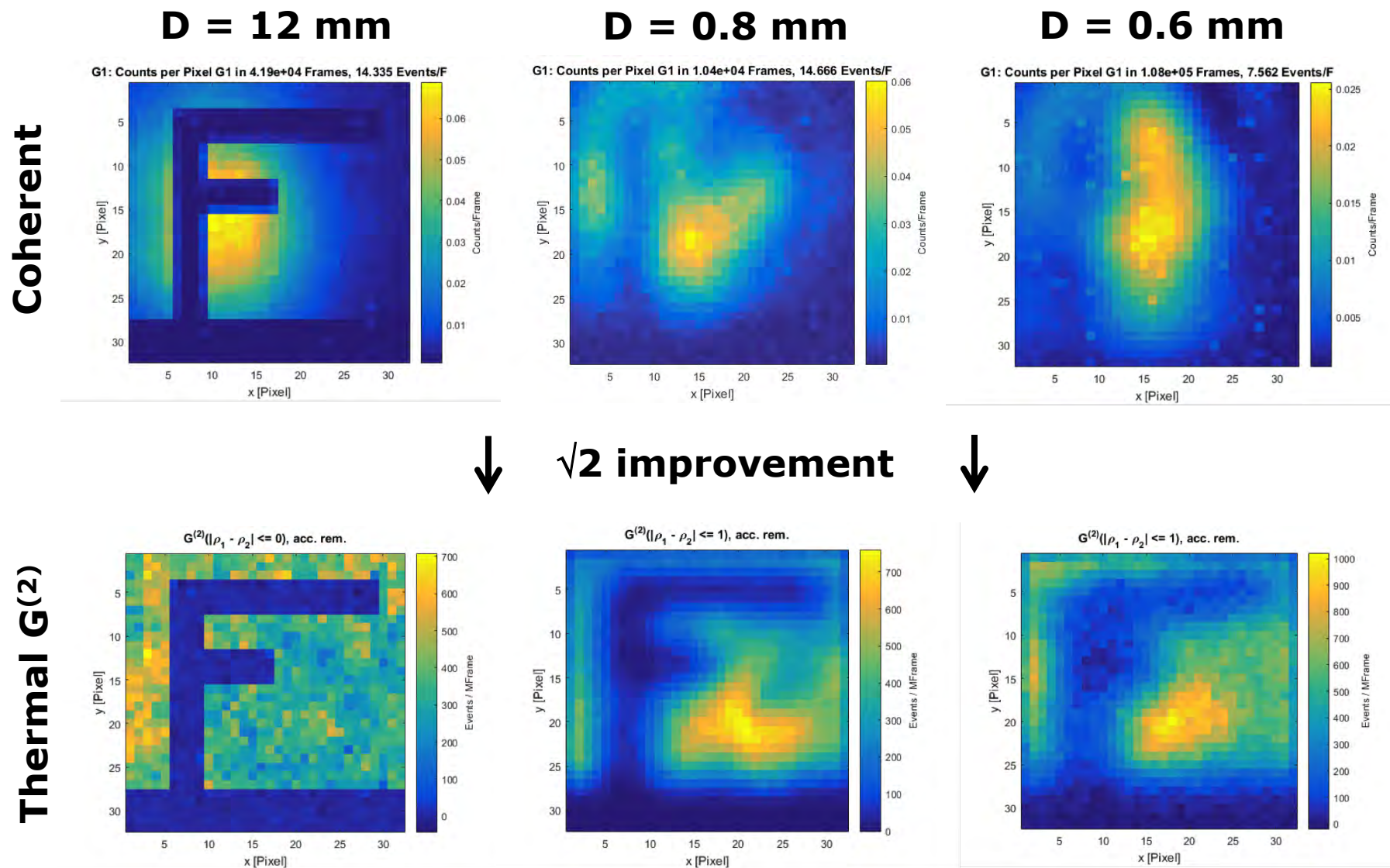


Higher Order $G^{(N)}$: Pseudo-Thermal Light Source

- Setup for thermal near-field imaging
- Rotating ground glass disk produces pseudothermal statistics



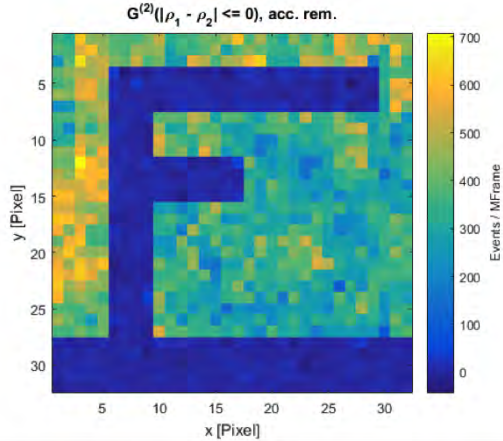
$G^{(2)}$ Measurement with Pseudo-thermal Light



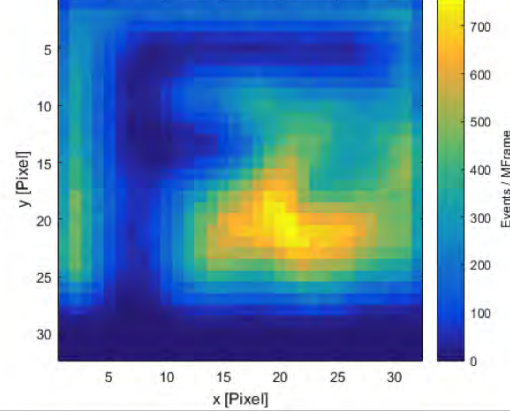
$G^{(3)}$ Measurement with Pseudo-thermal Light

D = 12 mm

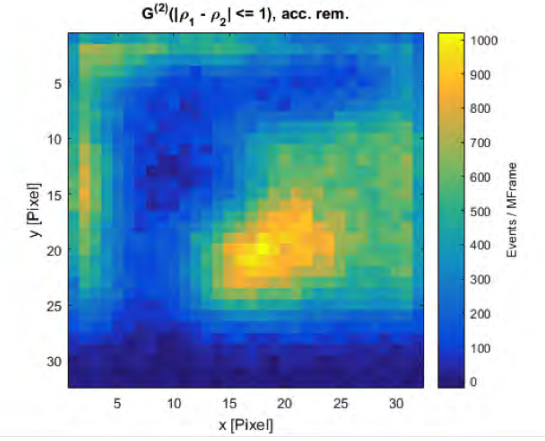
Thermal $G^{(2)}$



D = 0.8 mm



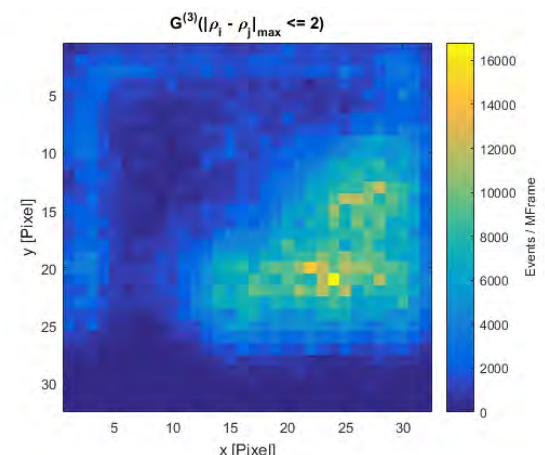
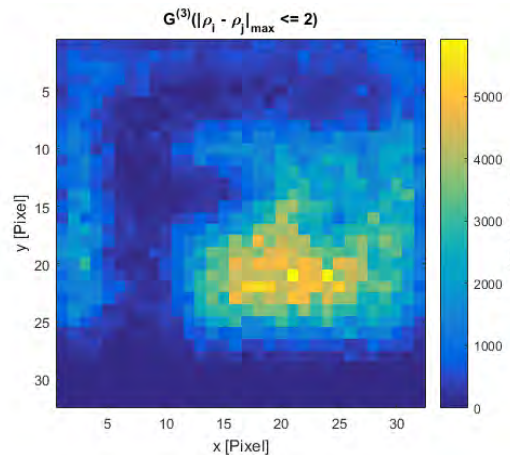
D = 0.6 mm



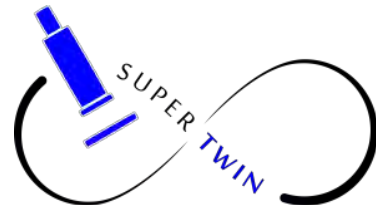
$$G^{(2)}(\rho, \rho)$$

↓ **no improvement!** ↓

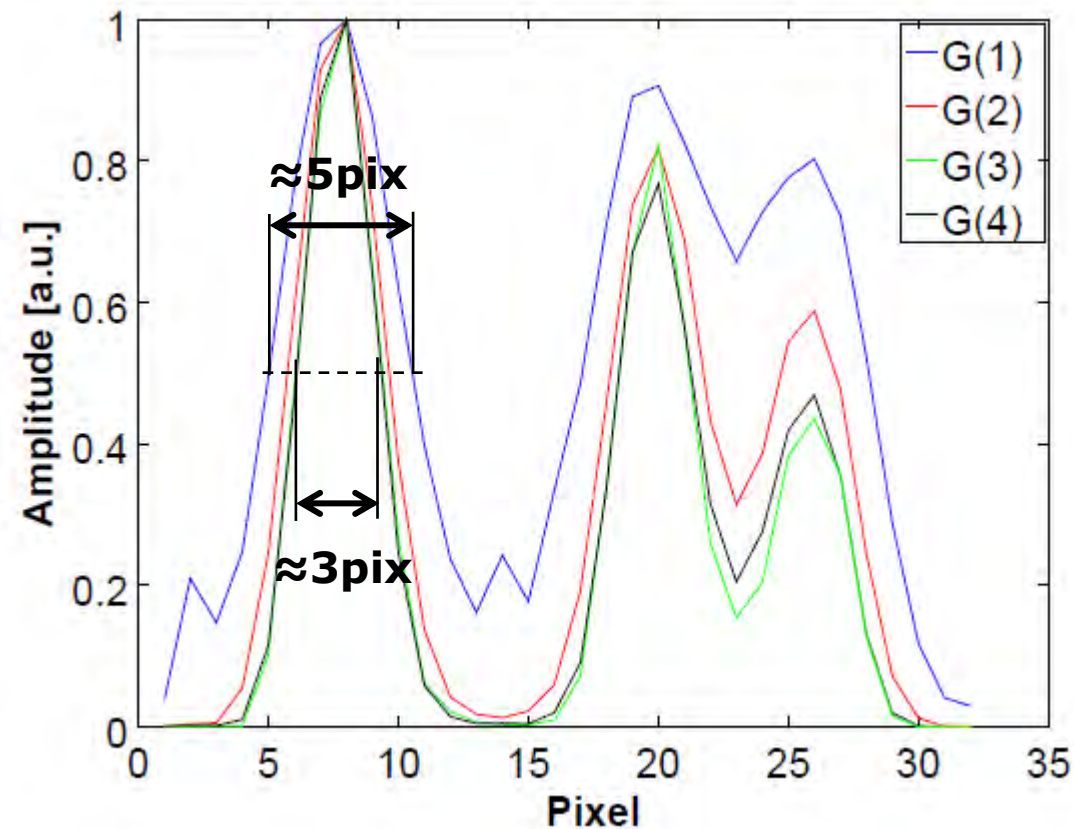
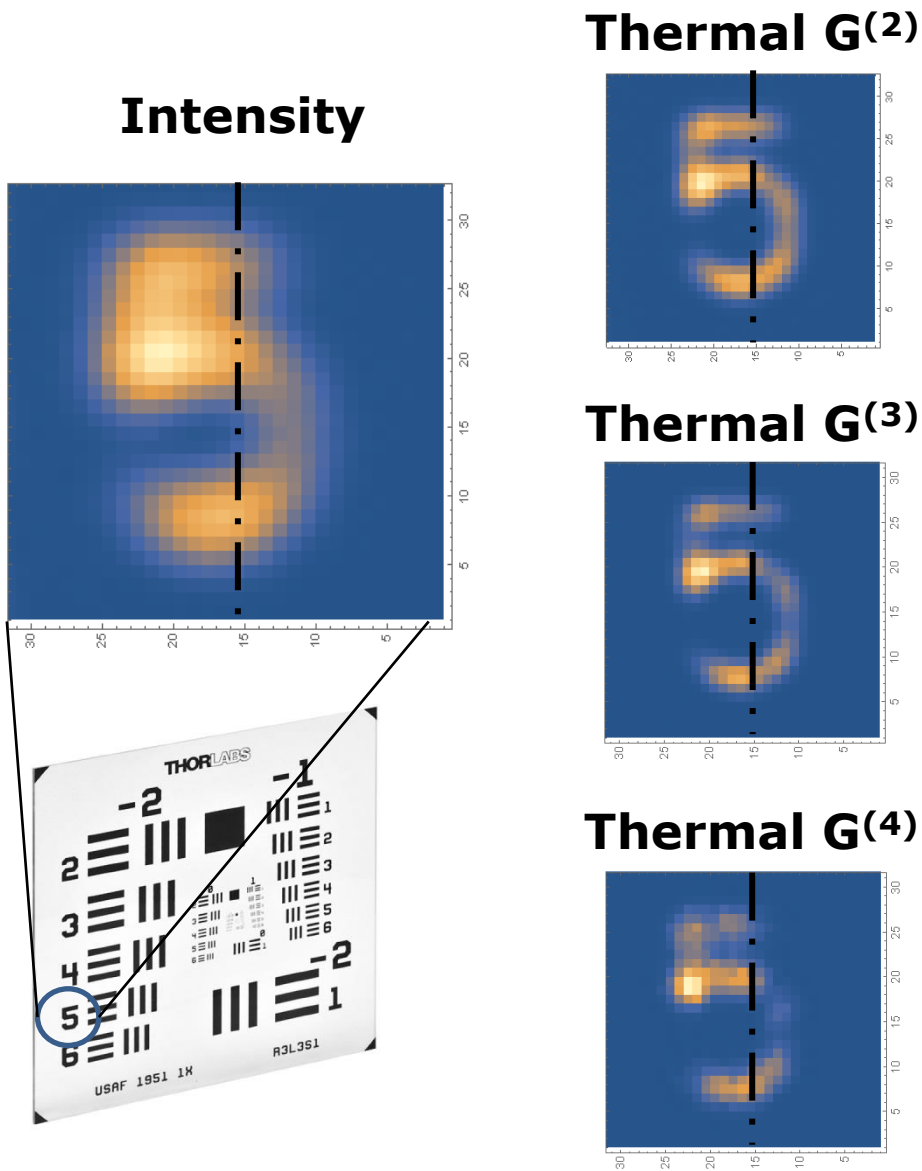
Thermal $G^{(3)}$



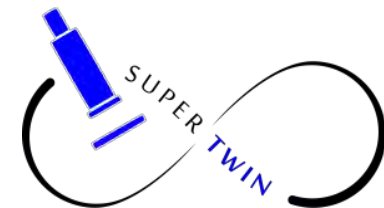
$$G^{(3)}(\rho, \rho, \rho)$$



Improvement Without Processing

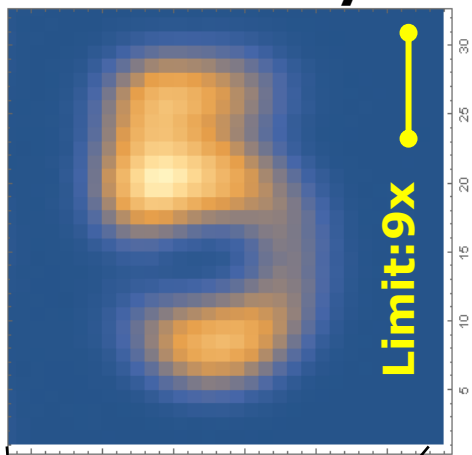


$G^{(N)}(\rho, \dots, \rho)$
diagonal
terms

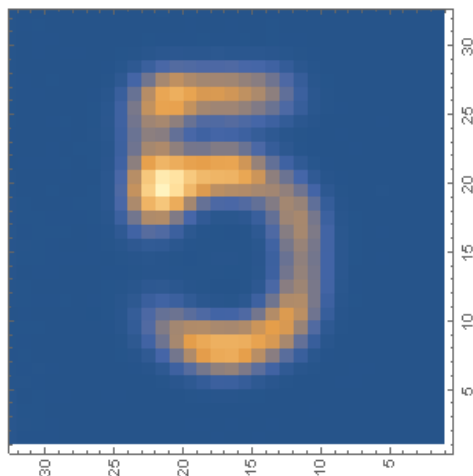


Applying Reconstruction Algorithm

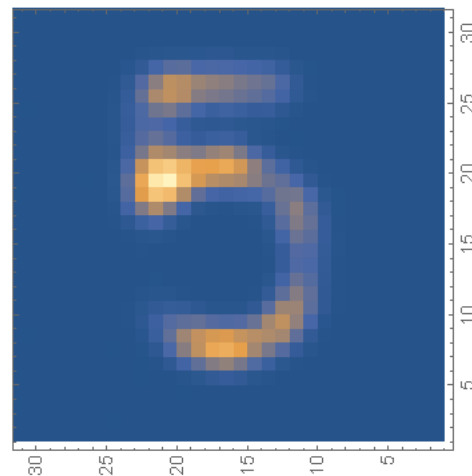
Limit: 9x
D=0.3mm
Intensity



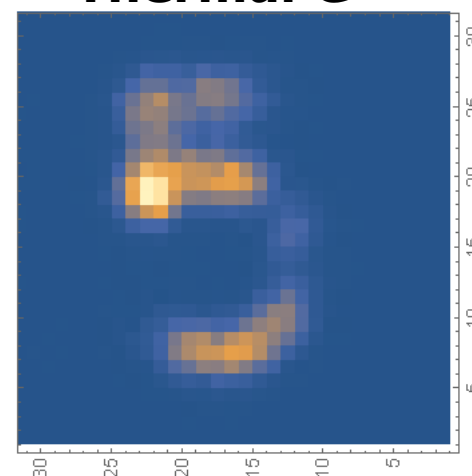
Limit: 5x
D=0.5mm
Thermal $G^{(2)}$



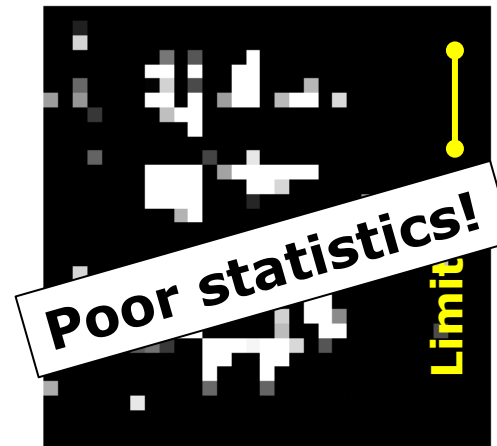
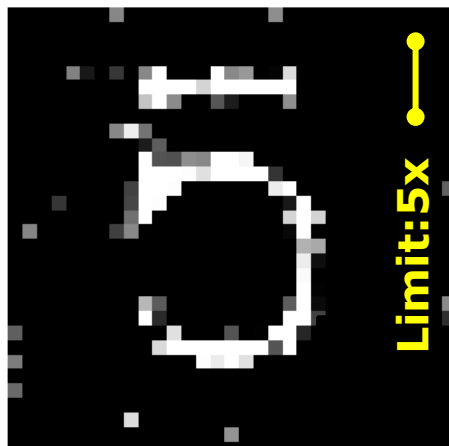
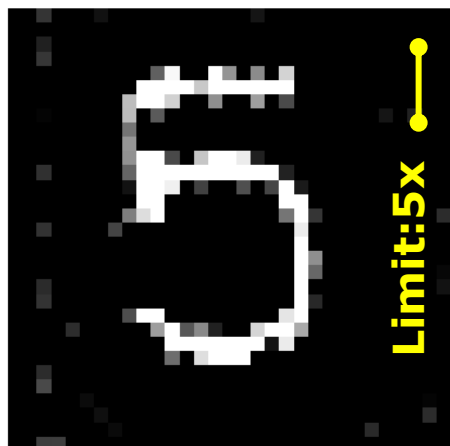
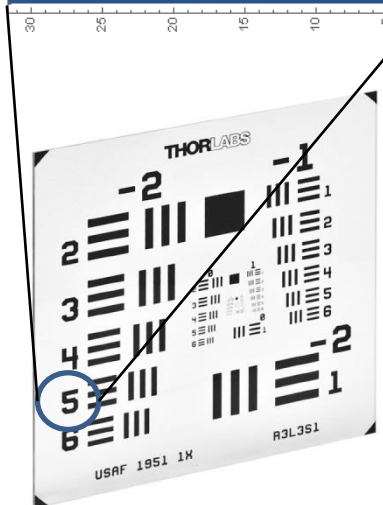
Limit: 5x
D=0.5mm
Thermal $G^{(3)}$



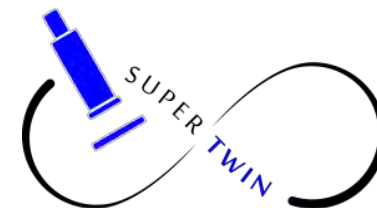
Limit: 7x
D=0.4mm
Thermal $G^{(4)}$



$G^{(N)} (\rho, \dots \rho)$
diagonal
terms

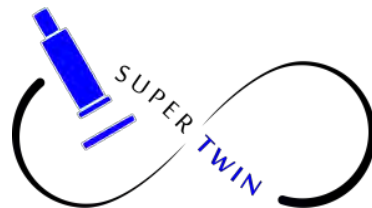


$G^{(N)} (\rho_1, \dots \rho_N)$
full
correlation



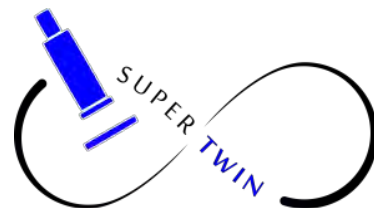
Outline

- Motivation
- Requirements for imaging with entangled photons
- SuperEllen fabrication and characterization
- $G^{(2)}$ correlations in SPDC with bi-photons
- $G^{(2)}$ - $G^{(4)}$ in thermal imaging
- Conclusions & future outlook



Conclusions & Outlook

- Superresolution concept addressed by entangled photon detection
 - Efficient detection of simultaneously impinging photons needs
 - TDC-based architecture
 - Thresholding mechanism
 - Efficient readout
- ➔
- **32x32 SPAD array demonstrator with per-pixel TDC and row/frame skipping**
 - **200ps timing resolution**
 - **20% fill-factor**
 - **800 kfps max**
 - Advantages are demonstrated in $G^{(2)}$ measurements of entangled photon pairs and $G^{(2)}$ - $G^{(4)}$ measurements with quasi-thermal light.
 - Future step: 256x256 detector for $G^{(5)}$ measurements





SUPERTWIN

All Solid-State Super-Twinning Photon Microscope

We thankfully acknowledge the support of the European Commission through the SUPERTWIN project, id. 686731.

