

SPAD arrays: from single-molecule detection to wide-field phasor fluorescence lifetime imaging

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UCLA



A brief history of past work

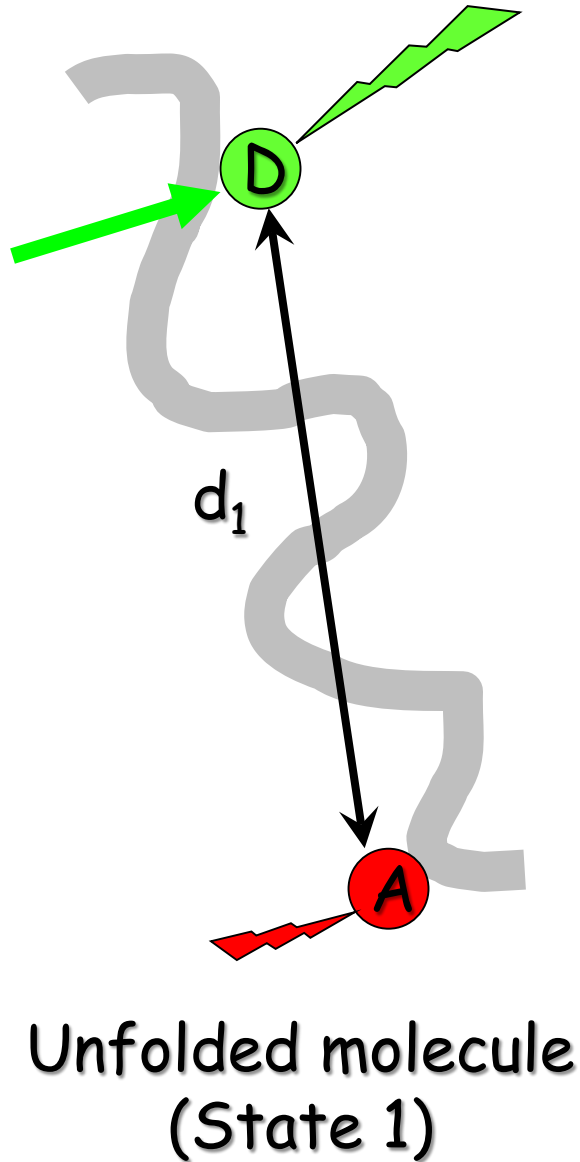
- 1996-2008: SPCM-AQR 14 (EG&G, Perkin-Elmer, Excelitas)
- 2008: single-pixel HPD: BiOS, *SPIE Proc.* 6862 (2008) 68620F
- 2010: 8x1 single-color FCS & burst detection: BiOS, *SPIE Proc.* 7571 (2010) 75710G
OptoE, *SPIE Proc.* 7608 (2010) 76082D
Biomed. Opt. Expr. 1 (2010) 1408
- 2011: 8x8 (of 32x32 SPADA) single-color FCS: BiOS, *SPIE Proc.* 7905 (2011) 790503
8x1 single-color FCS DSS, *SPIE Proc.* 8033 (2011) 803316
- 2012: 8x1 smFRET (4 spot): BiOS, *SPIE Proc.* 8228 (2012) 82280B
- 2013: 8x1 smFRET (8 spot): BiOS, *SPIE Proc.* 8590 (2013) 85900E
1 RE-SPAD (1 spot): BiOS, *SPIE Proc.* 8590 (2013) 85900D
- 2014: SwissSPAD: Photonics Europe, *SPIE Proc.* 9141 (2014) 914109
Opt. Expr. 22 (2014) 17573 + IISW 2013
- 2015: 4x12 single-color setup: DSS, *SPIE Proc.* 9492 (2015) 949204 (unpublished)
- 2016: sm file format: BiOS, *SPIE Proc.* 9714 (2016) 971405
- 2017: 16x1 single-color TCSPC: BiOS, *SPIE Proc.* 10071 (2017) 100710Q
more 8x1 smFRET + kinetics: *PLoS ONE* 12 (2017) e0175766
SwissSPAD 2: IISW 2017
- 2018: 4x12 smFRET (48 spots): *J. Chem. Phys.* 148 (2018) 123304 (+BiOS, unpublished)
4x12 CCF/crosstalk (48 spots): *NIMA*, DOI: 10.1016/j.nima.2017.11.070
smFRET review + perspectives: *Science* 359 (2018) eaan1133
SwissSPAD 2: BiOS, unpublished

Overview

1. Analysis of freely diffusing single molecules in solution
 1. Introduction
 2. Ideal detector requirements
 3. Current status
 4. Perspectives
2. Wide field imaging of single-molecules
 1. Introduction
 2. Ideal detector requirements
 3. Current Status
 4. Perspectives
3. *in vivo* NIR fluorescence lifetime imaging
 1. Introduction
 2. Ideal detector requirements
 3. Current Status
 4. Perspectives

1. Analysis of freely diffusing single molecules in solution

Förster Resonant Energy Transfer (FRET)

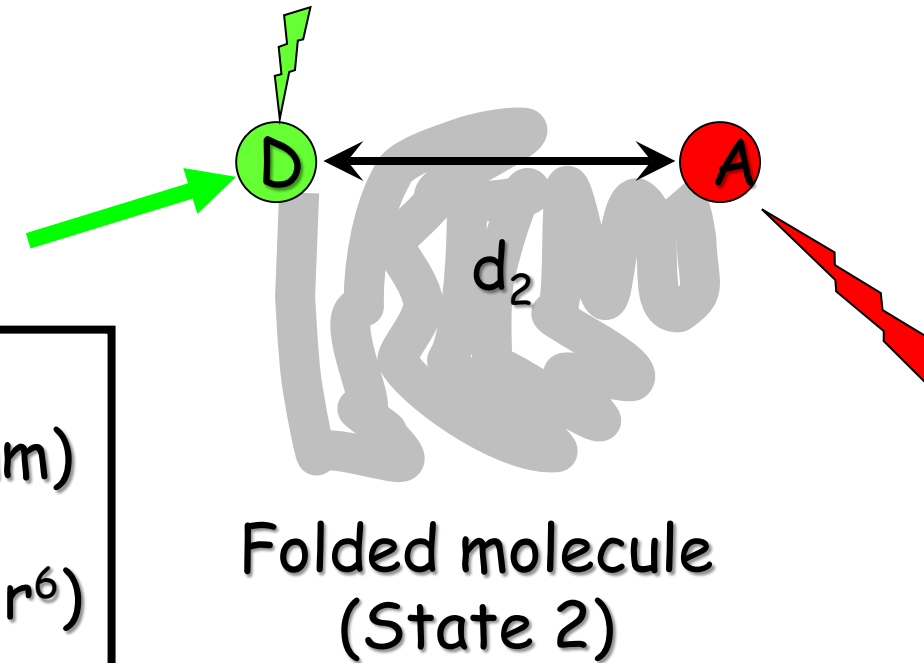


$$r = d/R_0$$

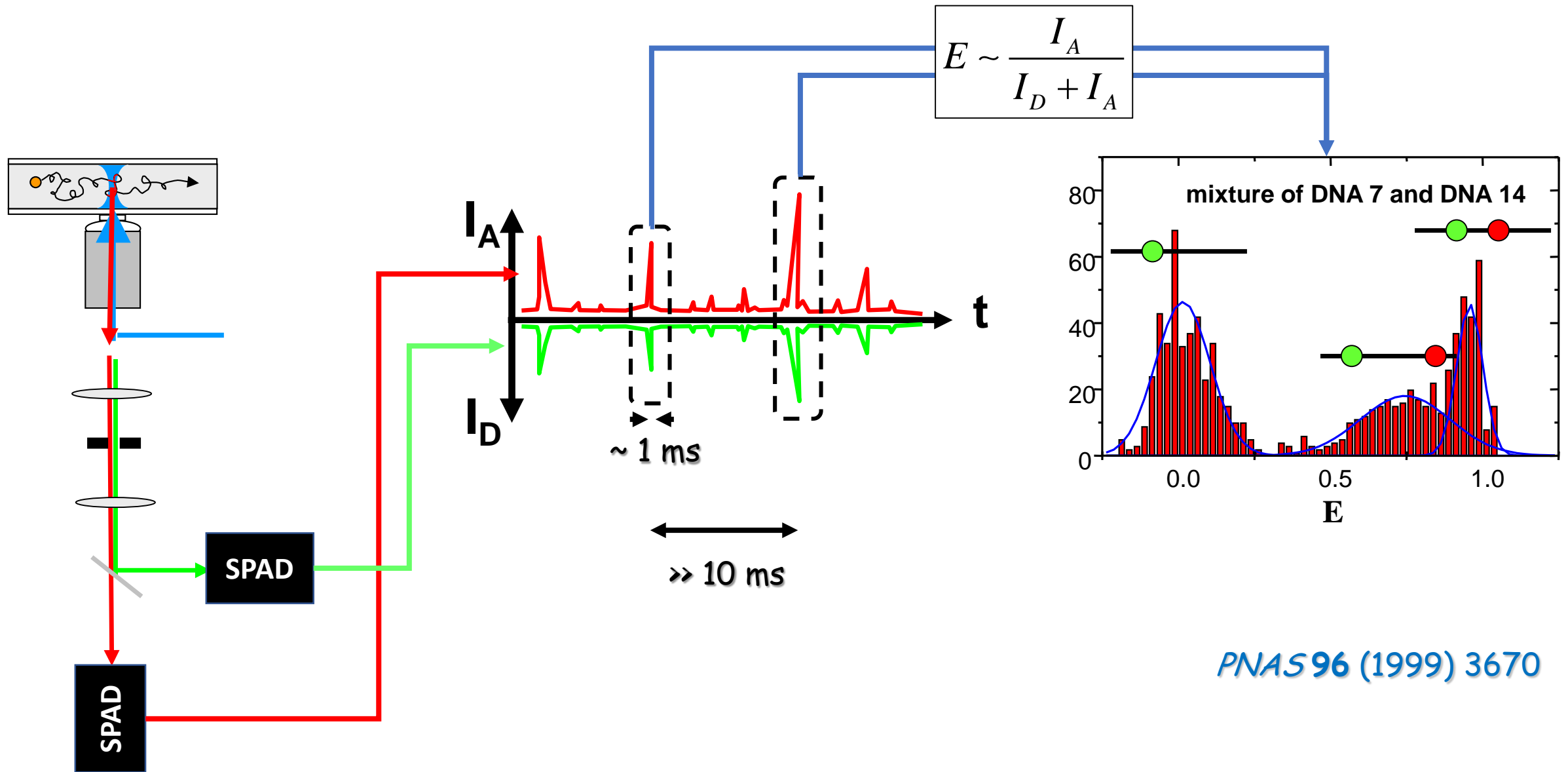
R_0 : Förster Radius (5-8 nm)

$$E = I_A / (I_A + I_D) = 1 / (1 + r^6)$$
$$= 1 - T_{DA} / T_D$$

E: Transfer efficiency



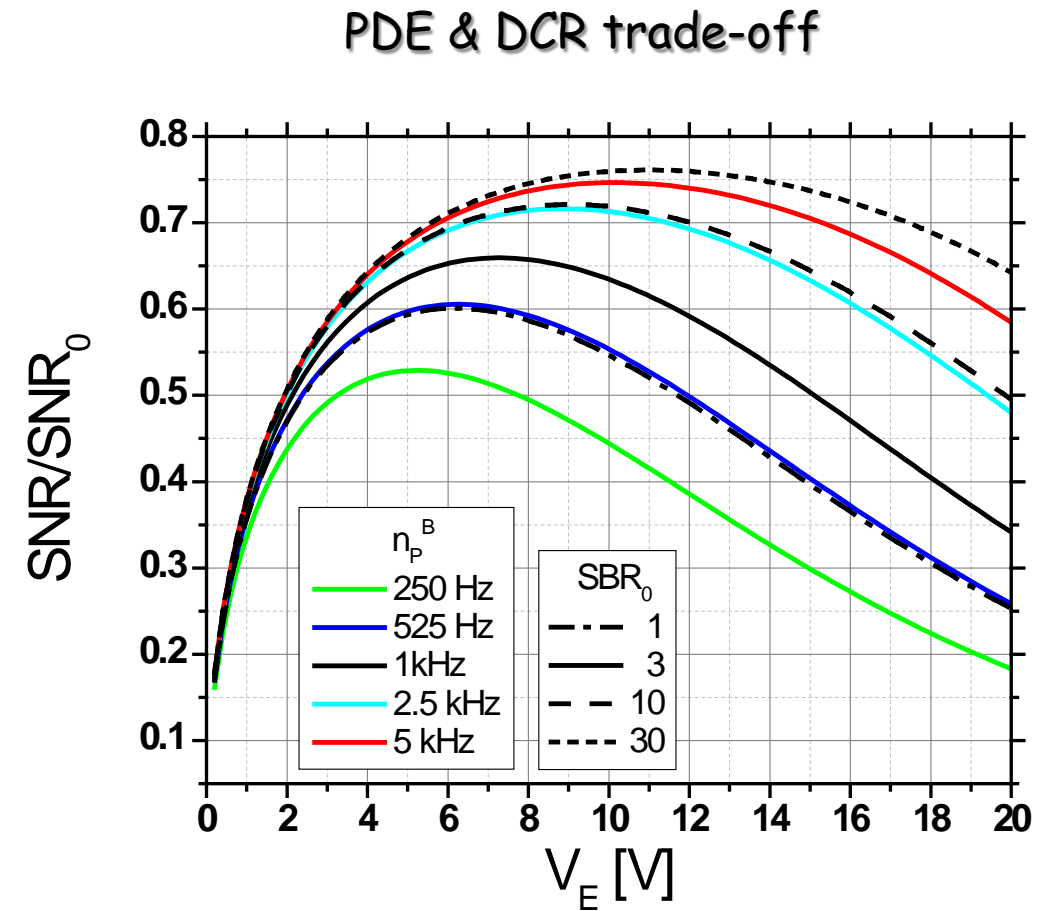
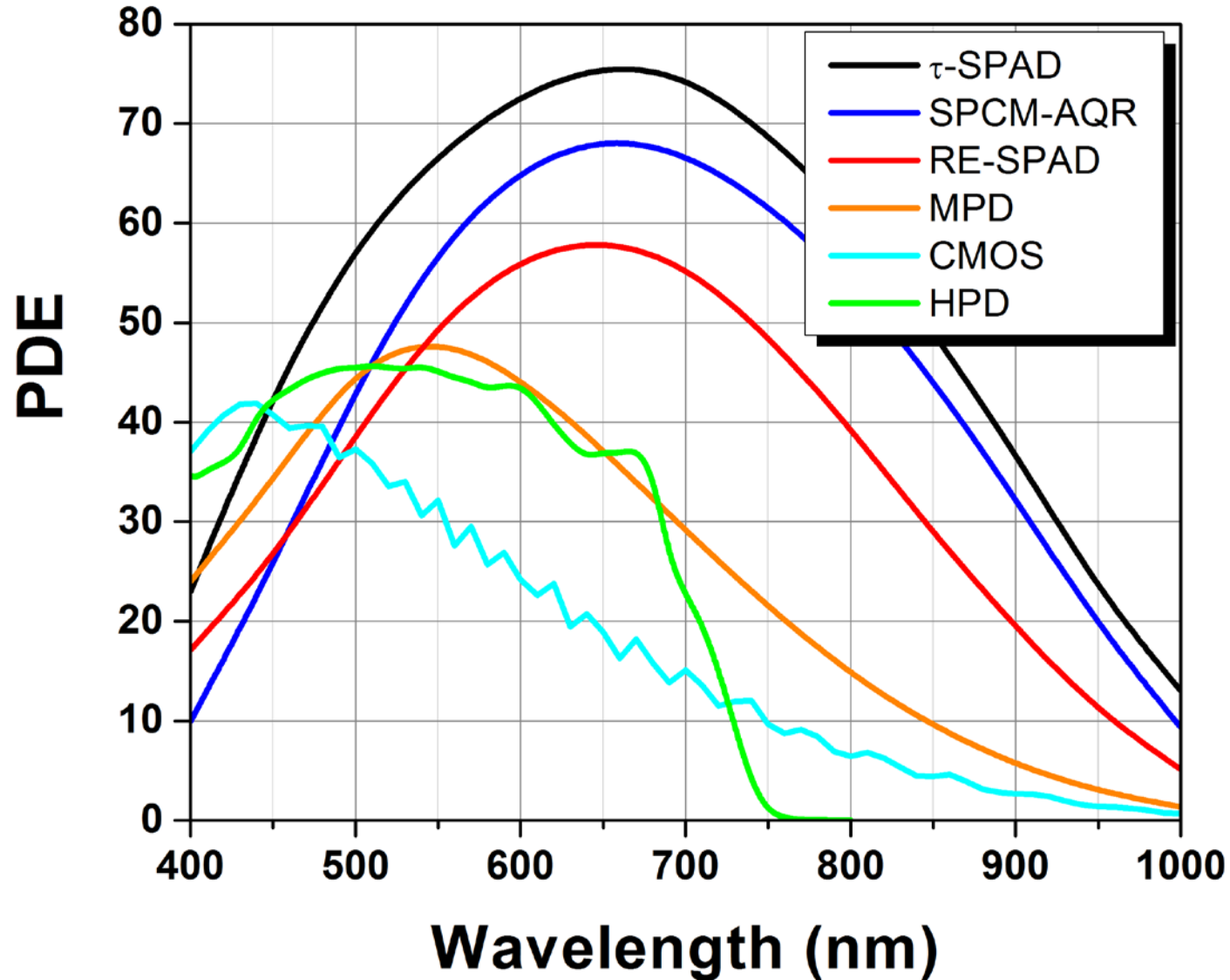
Single-molecule FRET Measurements: Principles



Detector Requirements

- Capture brief bursts of photons (0.1-10 ms, 10-500 ph)
 - Count rate < few MHz
 - Dead-time < 100 ns
- Time-correlated single-photon counting (TCSPC) capabilities
 - ~ 100 ps resolution (basic single burst analysis)
 - Laser repetition rate: 20-80 MHz
- Sensitivity:
 - Range: 500 nm-750 nm (Lasers: 488, 514, 532, 633, 690)
 - DCR < 1 kHz
- Afterpulsing, crosstalk:
 - As low as possible to allow for simple ACF/CCF analysis

PDE

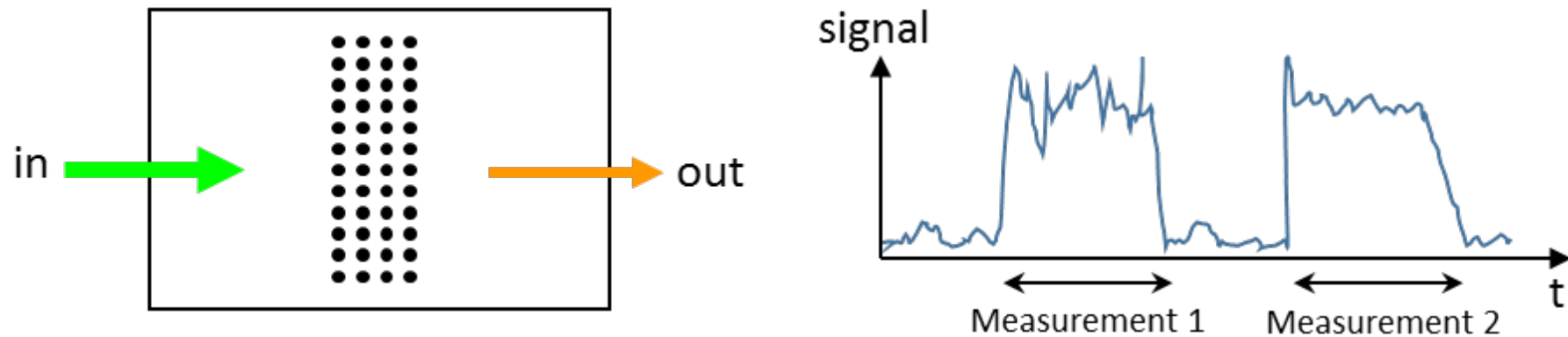


JSTQE 20 (2014) 3804420

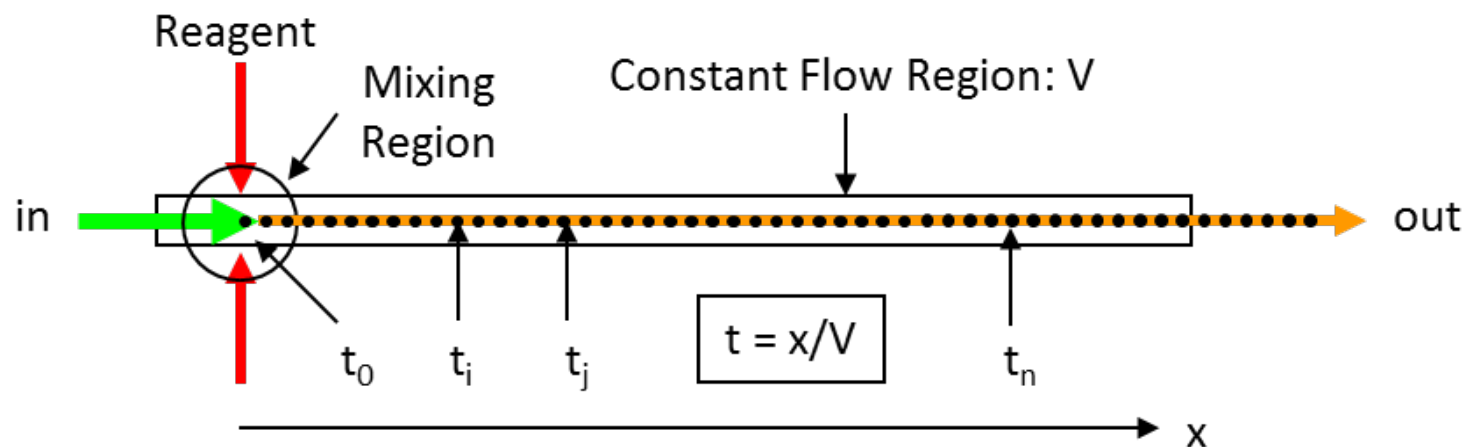
**Single-spot measurements are slow,
calling for parallelization**

Arrays: Measurement Geometries

1. "Formulator" principle (Mix & Monitor aka M&M)

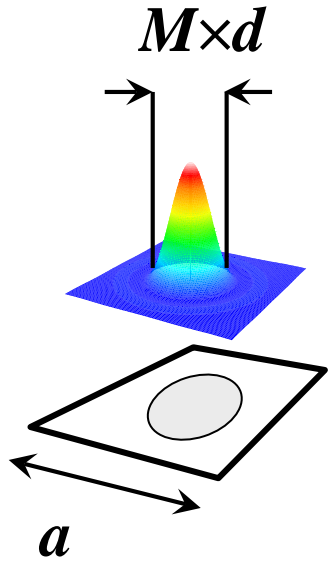


2. "Fast mixer" principle (Position = Time)



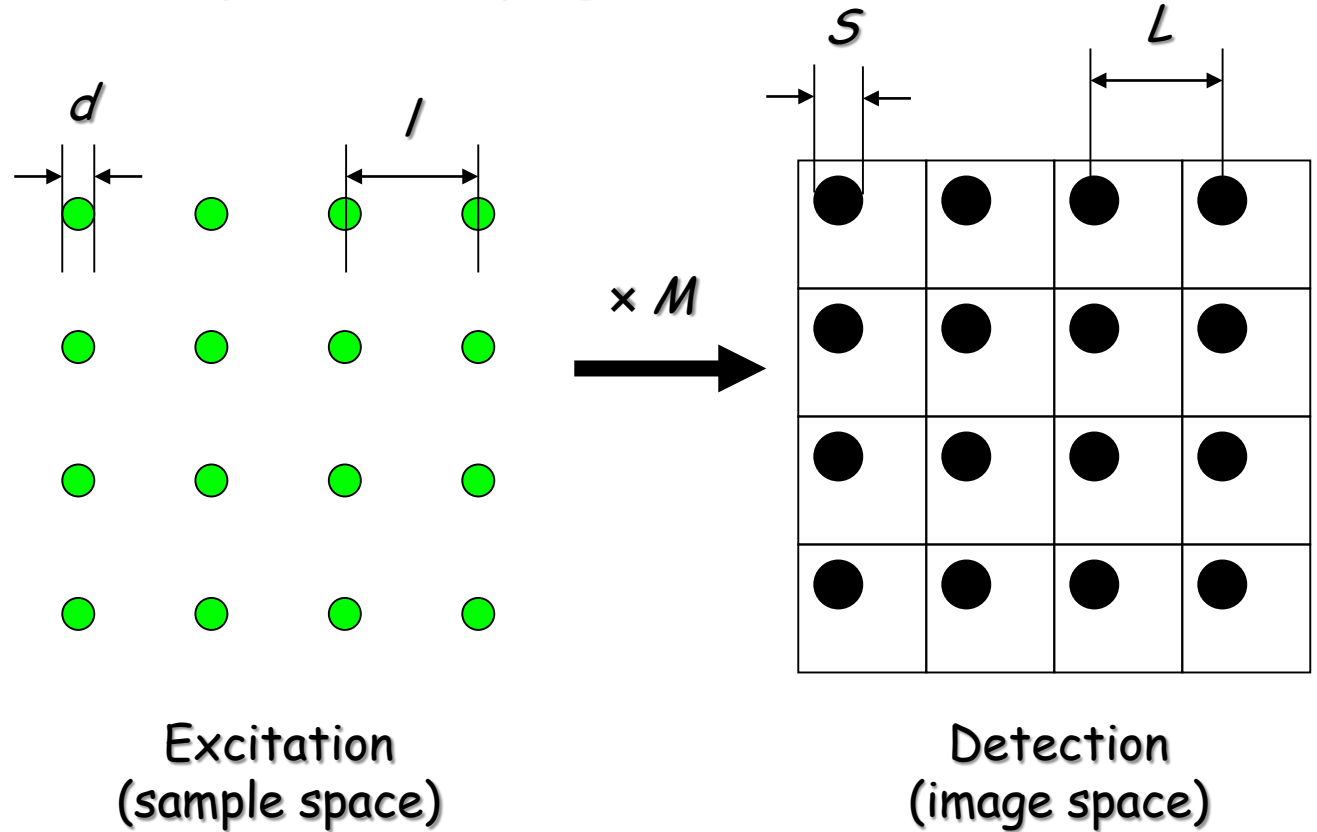
Detector geometry for high-throughput parallel smFRET

1. Confocal detection



$d \sim \lambda/NA \sim 0.5 \mu\text{m}$
 $M: 40 - 100$
 $a: 20 - 50 \mu\text{m}$

2. Independent sampling volumes



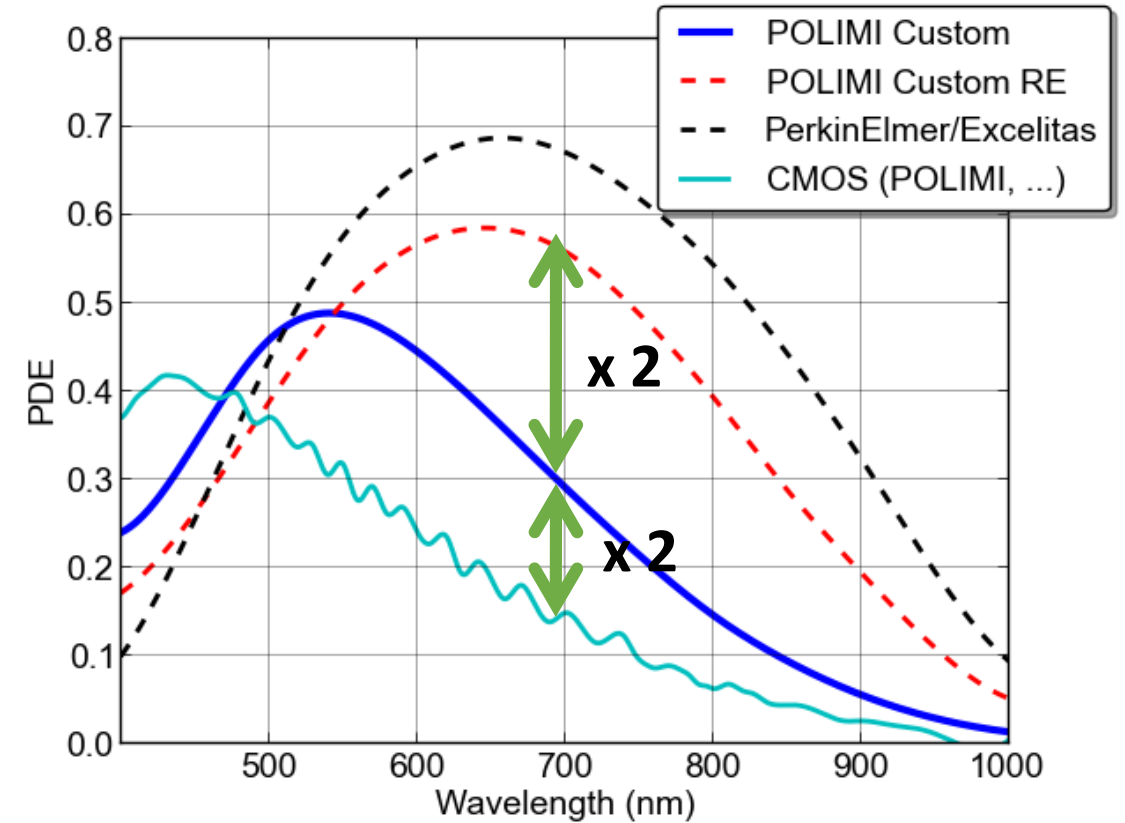
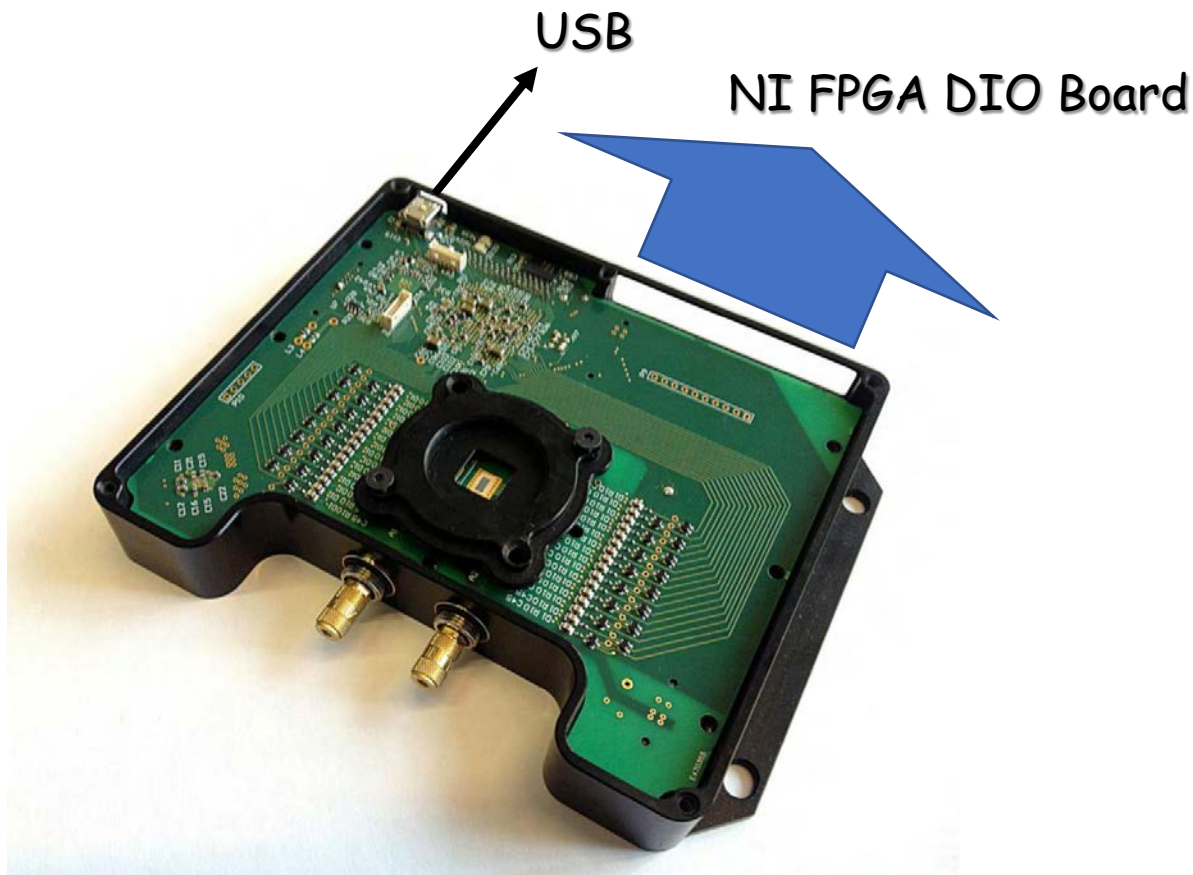
Excitation
(sample space)

$l \sim 5 \mu\text{m}$

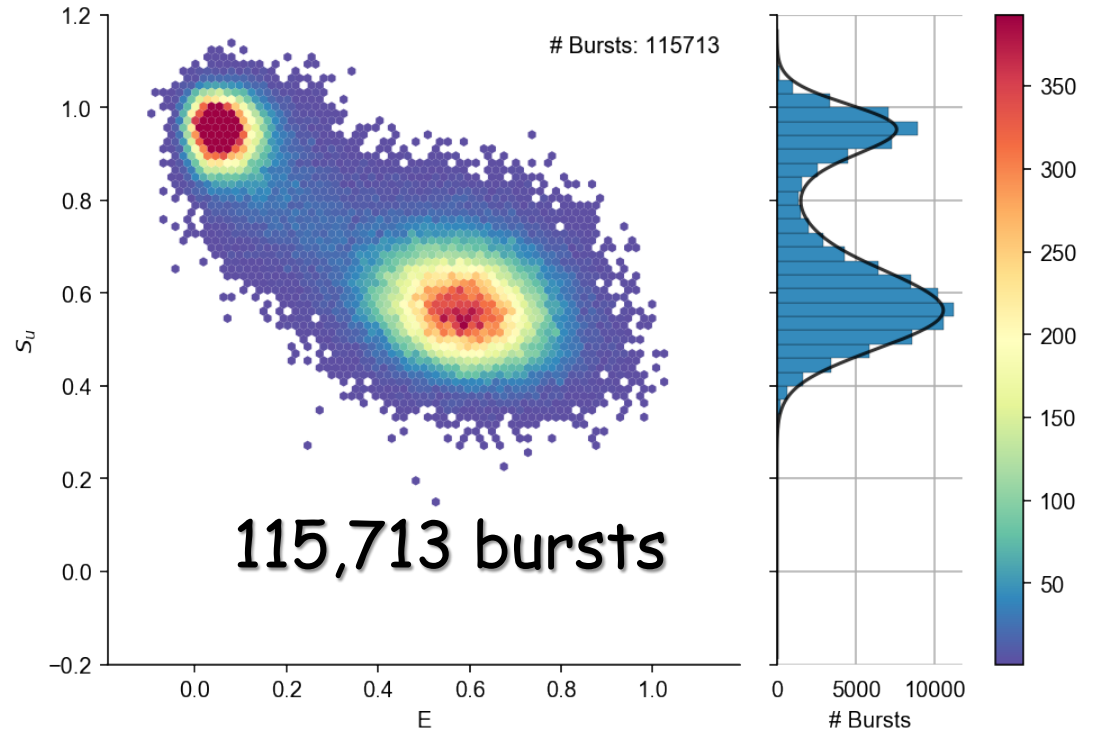
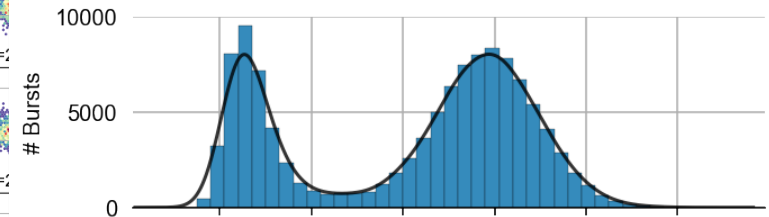
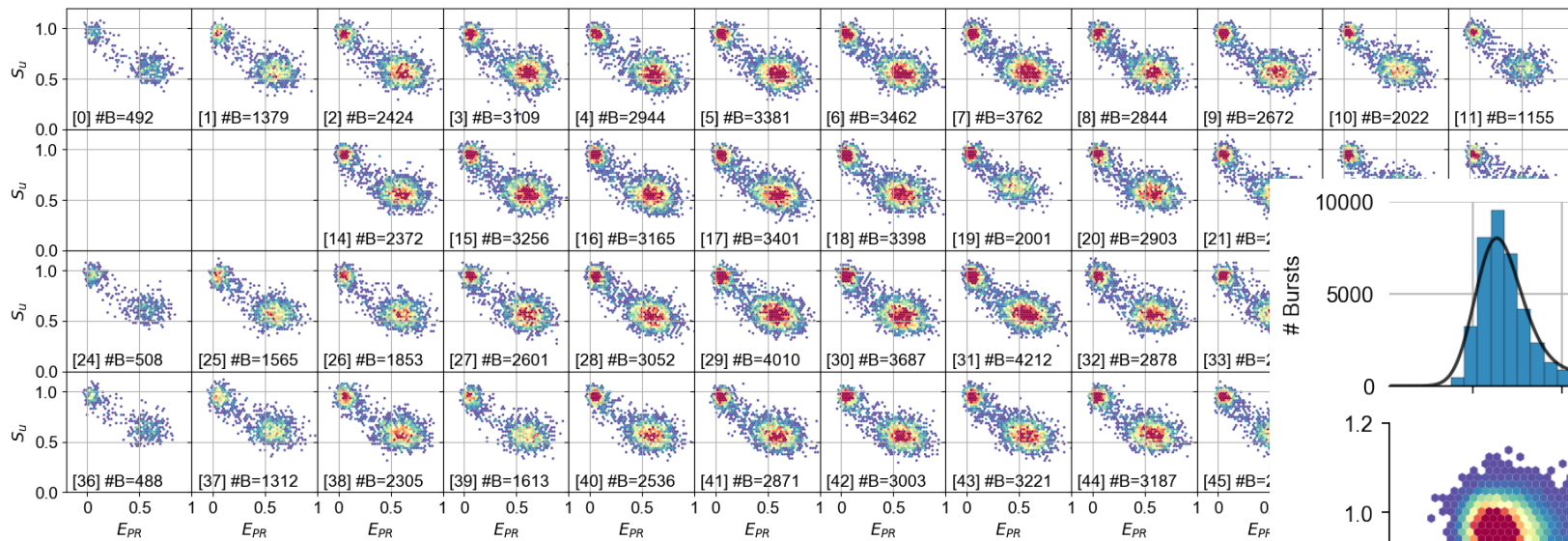
Detection
(image space)

Phil Trans R Soc B 368 (2013) 20120035

4x12 SPAD array in custom technology



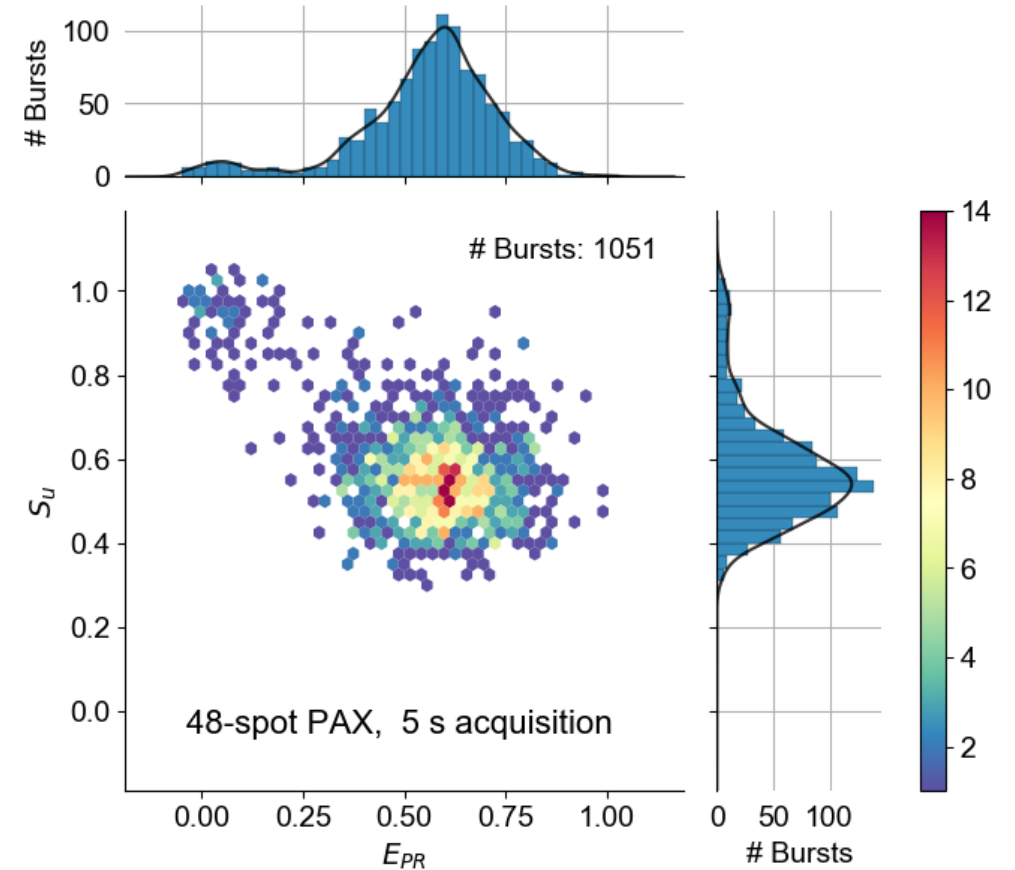
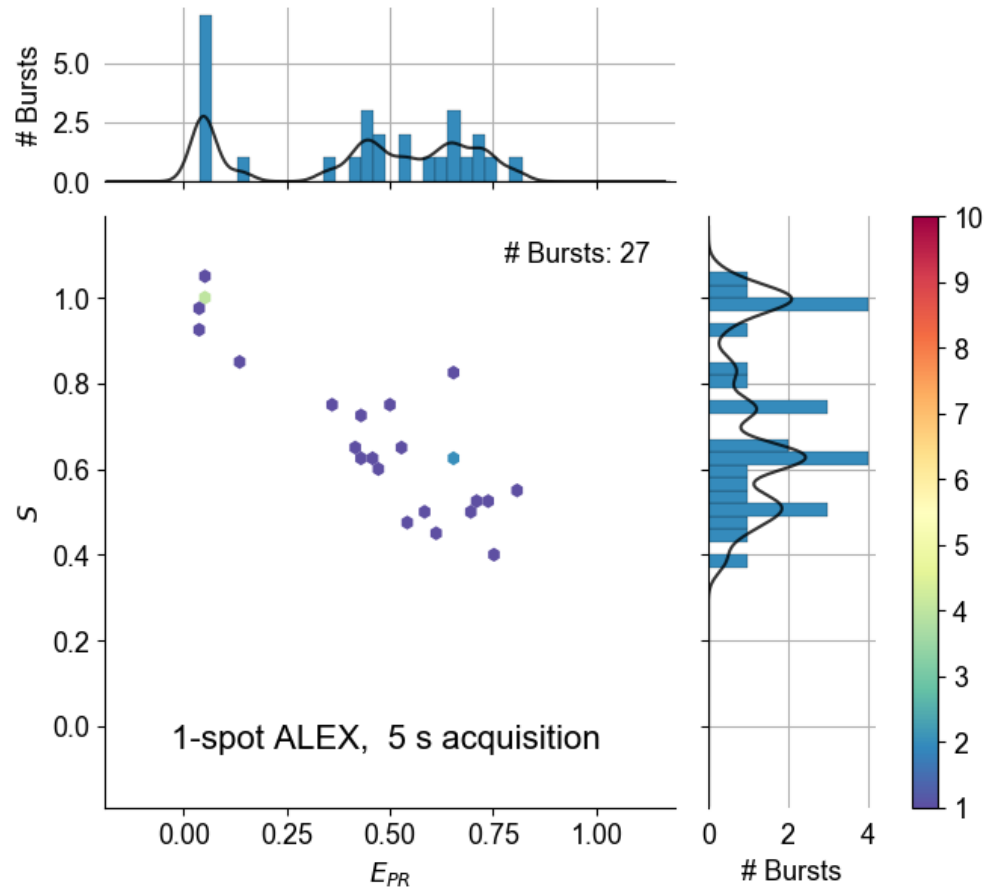
4x12 dsDNA measurements



Sample:

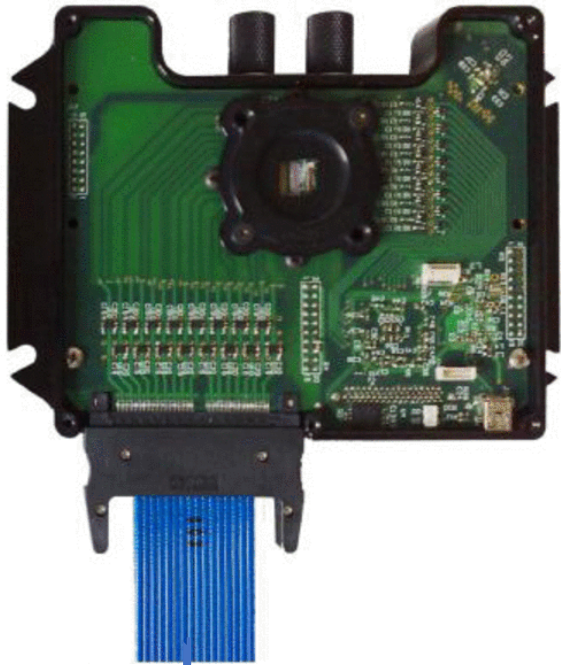
- 40 base-pair dsDNA
- 12-bp D-A separation
- D: ATTO550
- A: ATTO647N
- 10 min measurement

4x12 spots: towards 1 s dynamic resolution

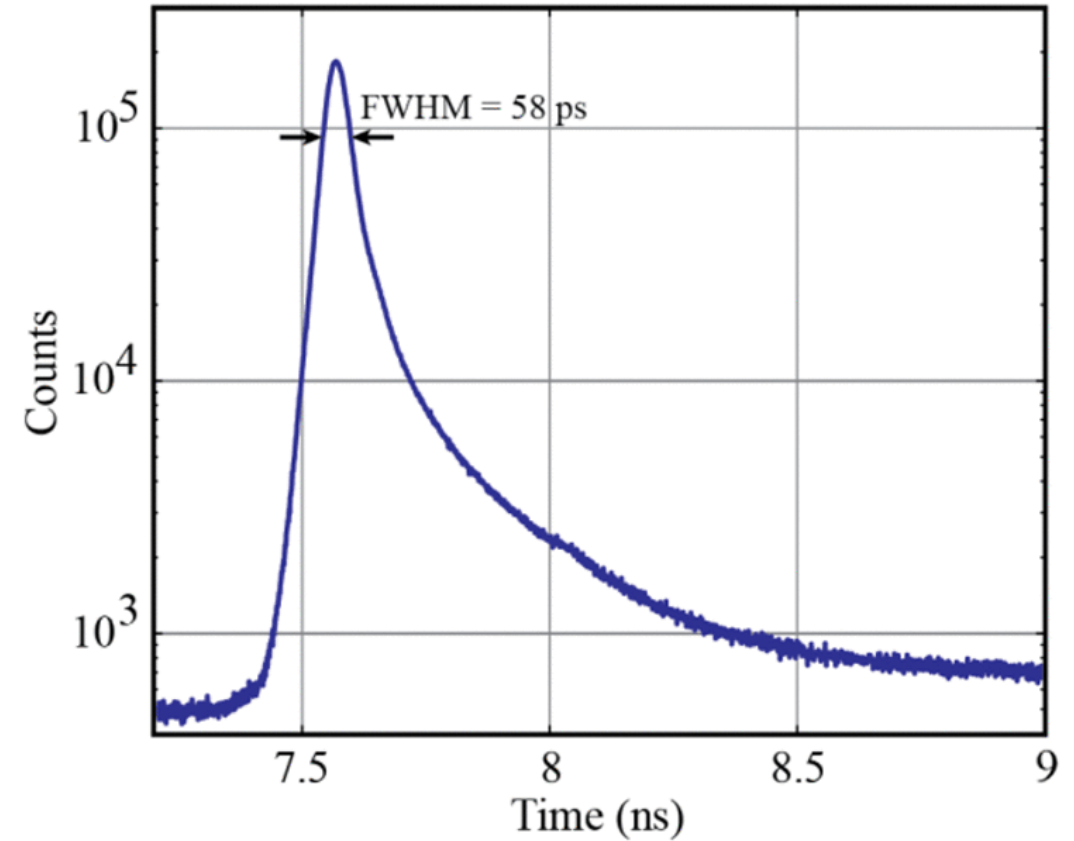


Linear TCSPC capable arrays

32 SPAD array
(custom RE process)



16 ch TCSPC
Hardware

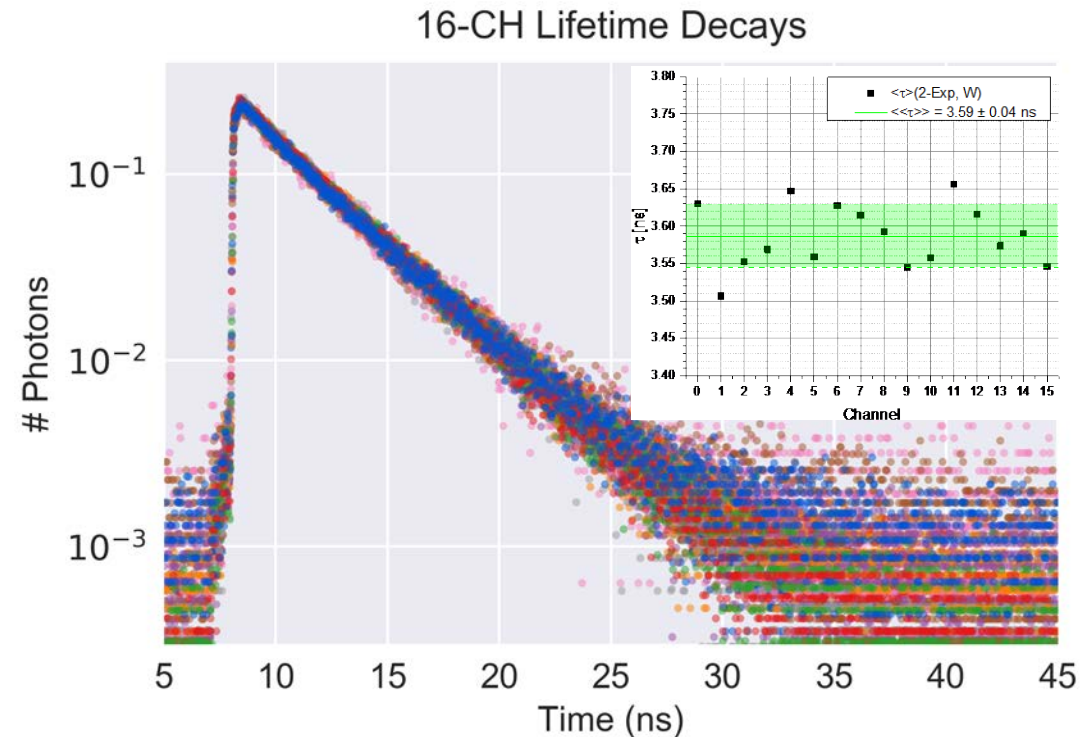
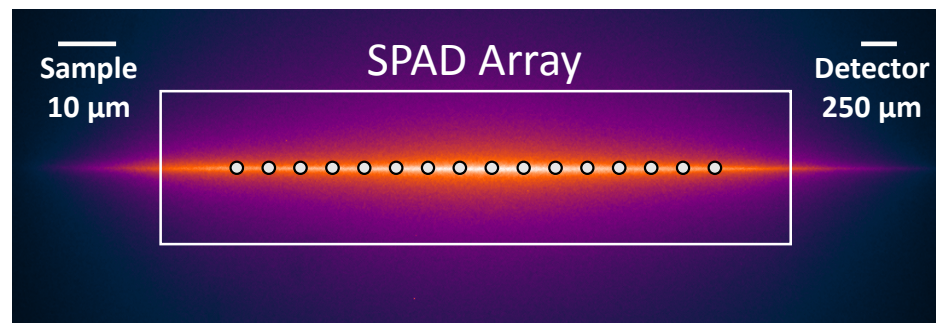
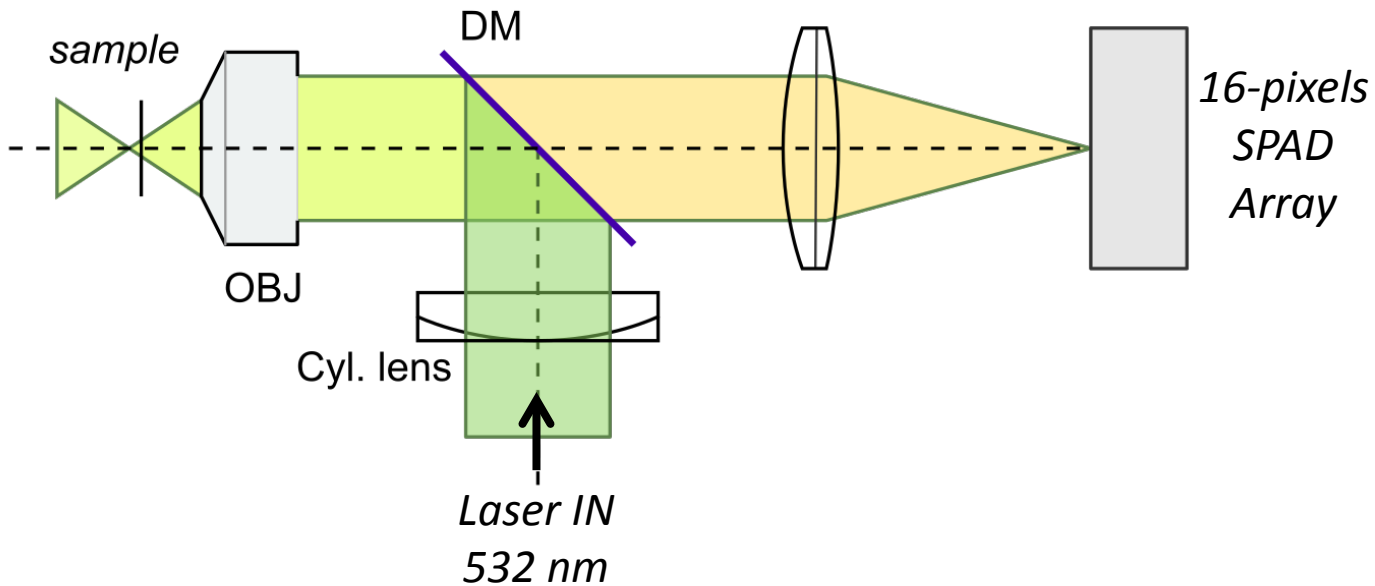


Pixel diameter: $50 \mu\text{m}$
Pixel pitch: $250 \mu\text{m}$
Geometry: 32×1

Antonioli *et al.* *Rev. Sci. Instrum.* **84**, 064705 (2013)
Cuccato *et al.* *IEEE Photonics J.* **5**(5) (2013)

Linear geometry for mixer experiments: 32x1 TCSPC capable arrays

Time-resolved measurement provide access to information inaccessible in mere counting measurements



80 base pairs dsDNA + ATTO550

Proc. SPIE 10071 (2017) 100710Q

Conclusion & Perspectives (1)

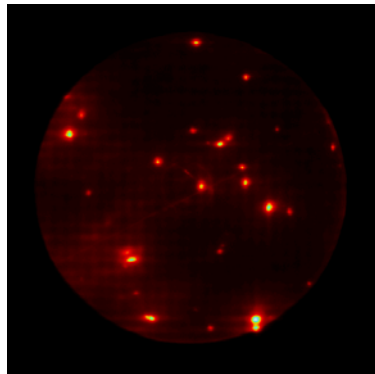
- Red-enhanced version of SPAD arrays will allow faster measurements (and potentially extend the spectral range of usable dyes)
- TCSPC capabilities are useful but not always necessary (and require high power lasers)
- 3D architecture for larger arrays (256x1, 32x32, larger? but for what applications?)
- New illumination & detection schemes needed to afford larger fields of views
- User modifiable FPGA firmware (or auxiliary NI FPGA?) for data preprocessing

3. *in vivo* NIR fluorescence lifetime imaging

Similarities & differences between single-molecule imaging and small animal imaging

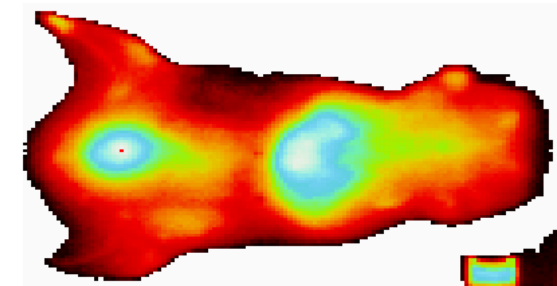
smFRET

- Fluorescence in the visible ($500 < \lambda < 750$ nm)
- Weak and sparse signals
- High fill factor needed
- Low dynamic range, high peak count rate
- Short observation timescales (high resolution macrotime needed)
- Long lifetimes (> 1 ns)
- Narrow IRF (SPAD is often dominating, but rarely an issue)



Small animal FLI

- NIR to SWIR
- Spatially extended signal, generally weak
- High fill factor needed
- Low dynamic range but potentially high peak count rate (adjustable by I_{ex})
- No need for high resolution time scale (< 0.1 s is enough to counterbalance breathing artefacts)
- Very short lifetimes (< 1 ns)
- Lots of scattering resulting in broad and spatially dependent IRF



Sparse vs Uniform signal

SPADs in detector: N
"on" SPADs at any time (on average): P
Macrotime stamp resolution: dt
or
Frame readout time: Δt

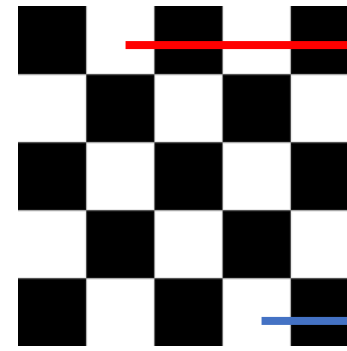
Event-driven readout encoding (per pixel):

- S bytes to encode SPAD position
- T bytes to encode macrotime
- L bytes to encode nanotime

Example:

- $S+T+L = 8$
- 1,000 sm at 10 kHz = 10 Mcps = P/dt

Bandwidth = 80 MB/s



S, T, L

Readout Bandwidth:
 $P(S+T+L)/dt$

L

Readout Bandwidth:
 $NL/\Delta t$

1-bit frame readout encoding:

- L bytes to encode nanotime
- Frame rate: $1/\Delta t$

Example:

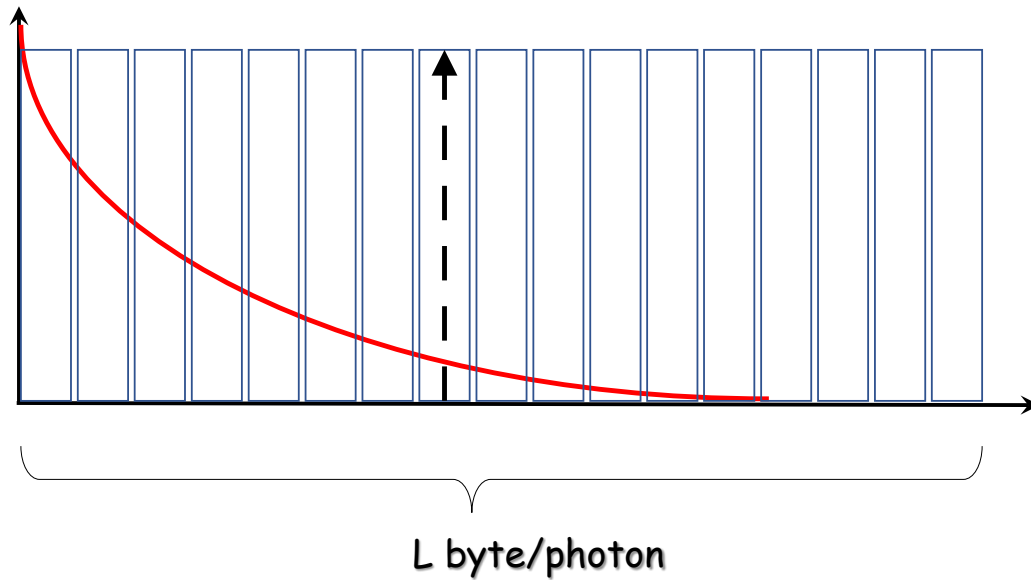
- $L = 1/8$ (1 bit), $N = 1M$
- $\Delta t = 10$ us (max count rate/pixel \ll 100 kHz)
- 1 frame = $N/8$ bytes = 125KB

Bandwidth = 12.5 GB/s most of which are 0

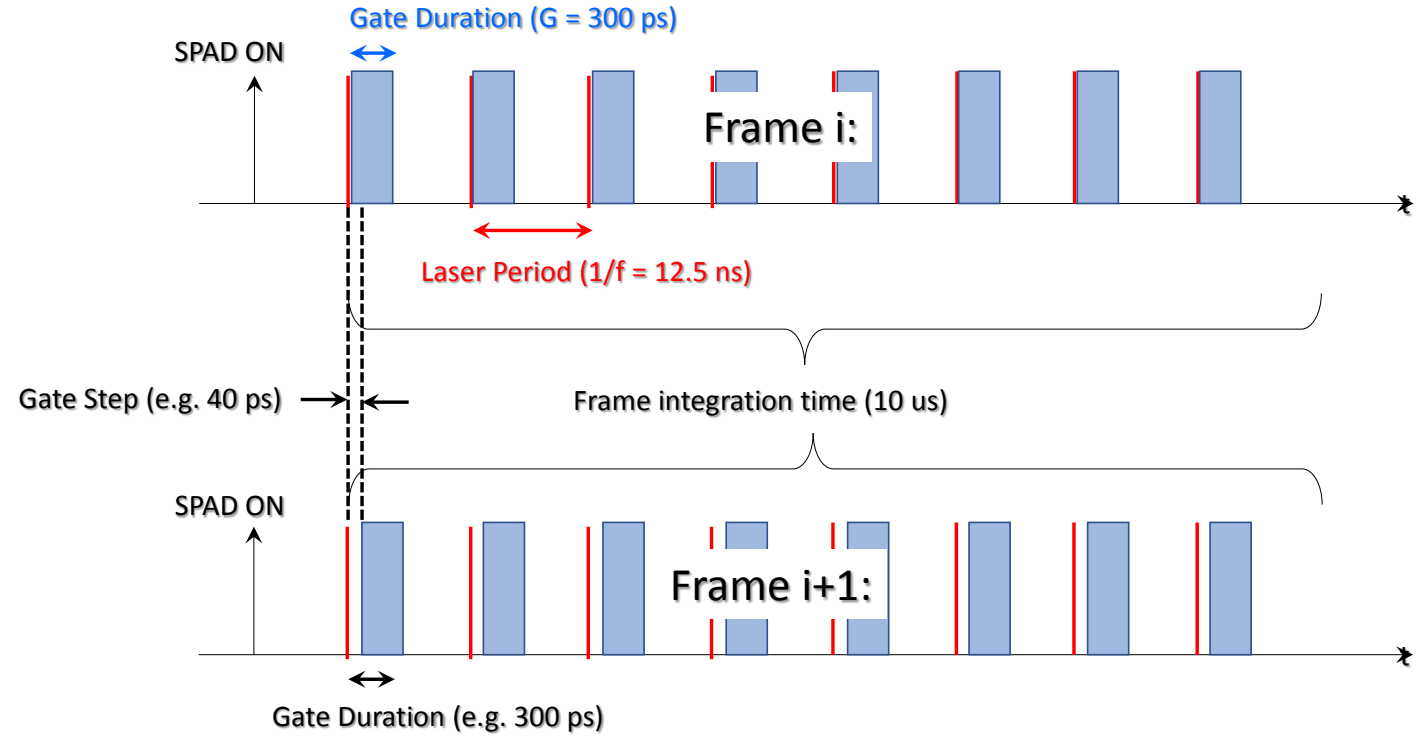
TCSPC

vs

Gated

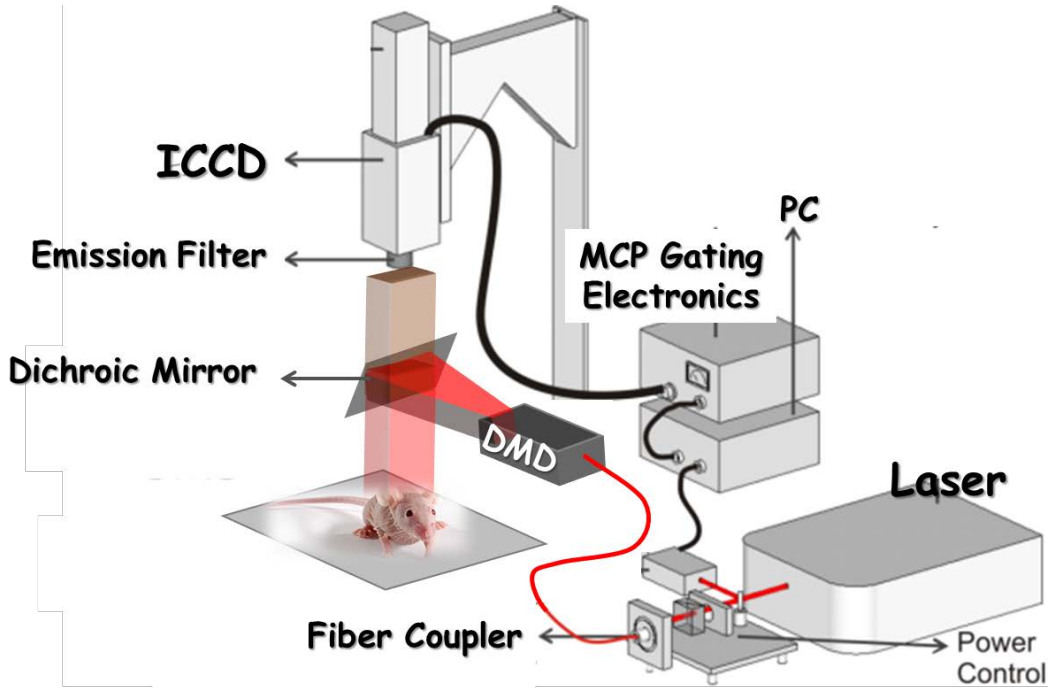


Very demanding technologically
and in bandwidth.

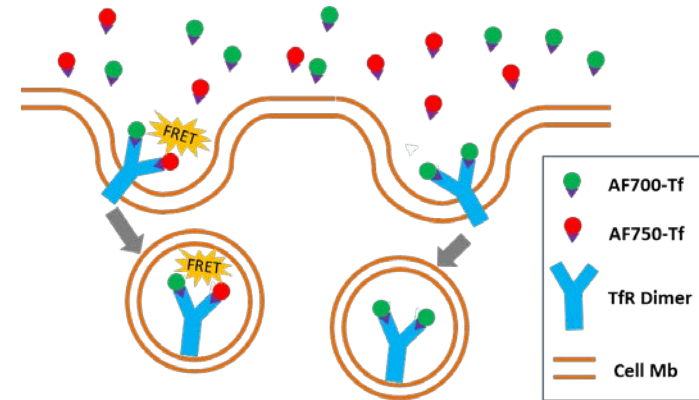
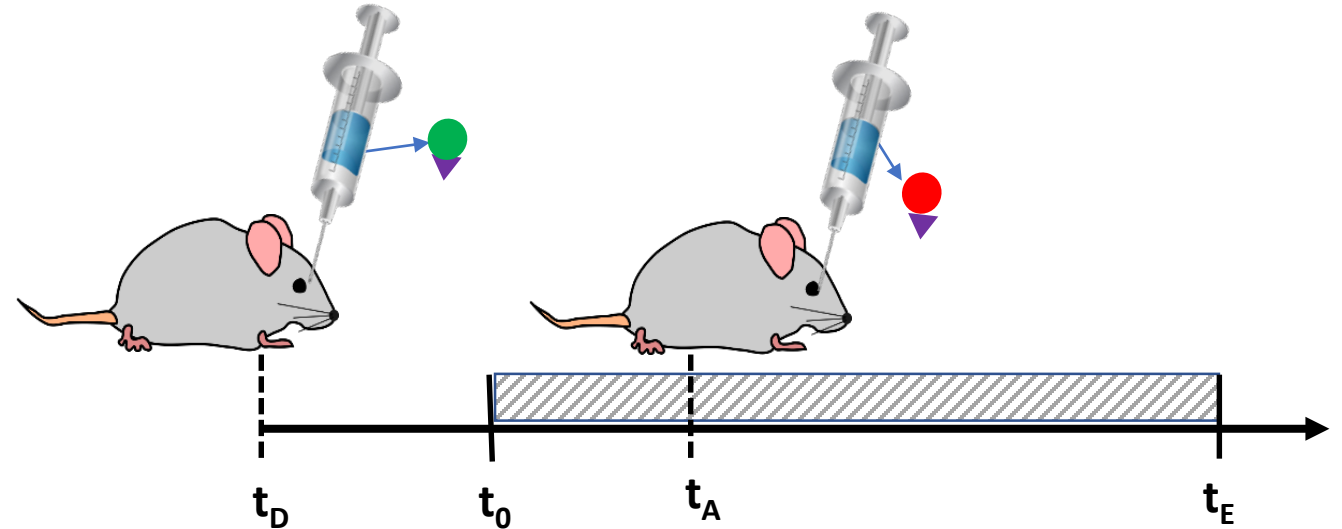


Wasteful acquisition
(e.g. detector is on $G \times f = 2.4\%$ of the acquisition)

in vivo NIR FRET fluorescence lifetime analysis



Gate: 300 ps
Step: 40 ps
Integration: >100 ms

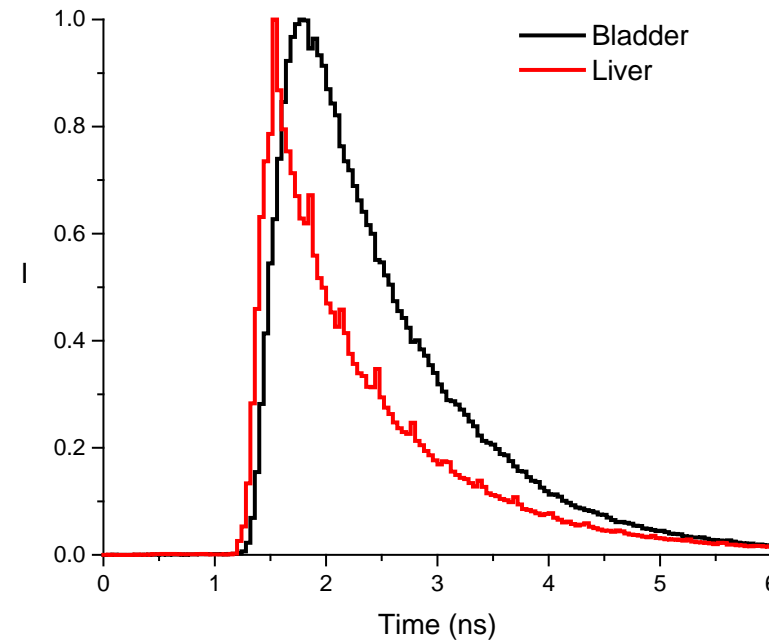
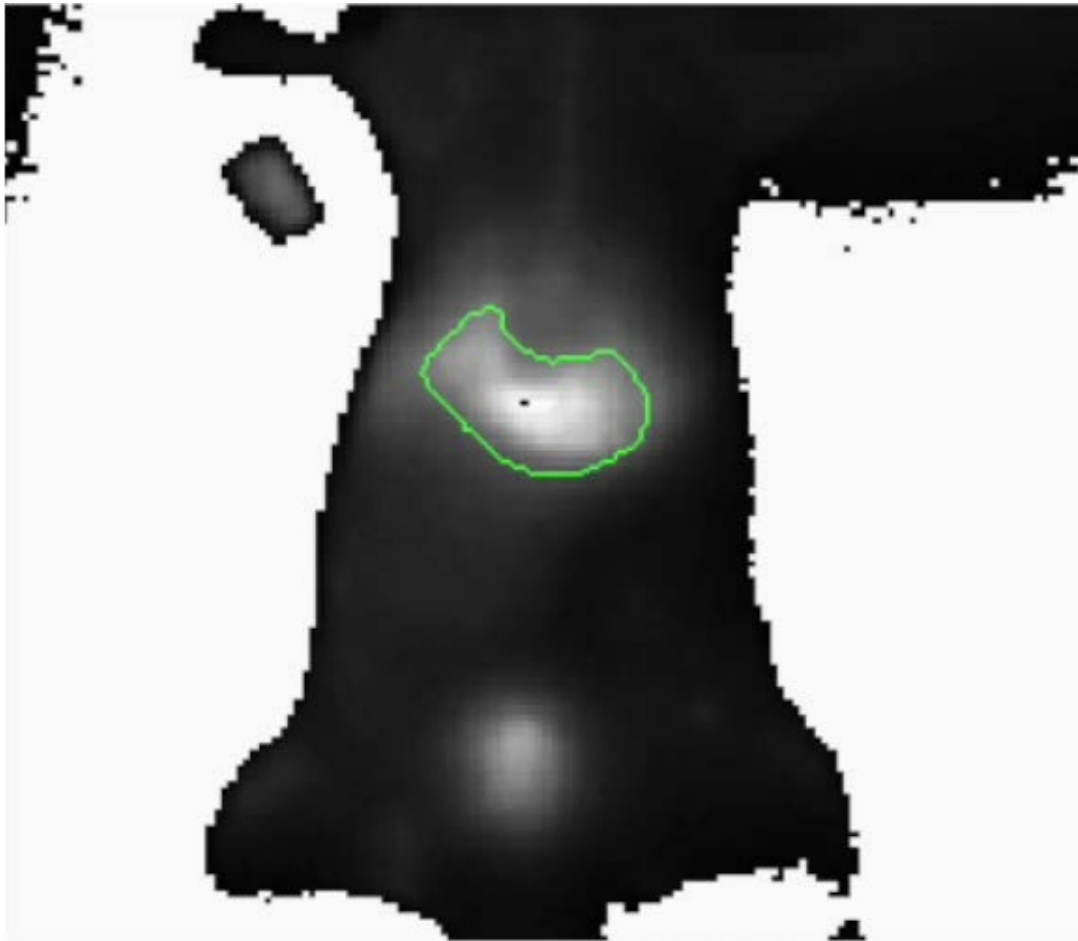


$$\tau_{DA} = \tau_D (1 - E) < \tau_D$$

in collaboration with the Intes & Barroso Labs

Chen et al., *BiOS* 2018, 10487-17, *in preparation*

FRET analysis by decay fitting



$$\tau_1 = \tau_{DA}$$

$$\tau_2 = \tau_D$$

$$f(t) = N_1 \frac{1}{\tau_1} \exp\left(-\frac{t}{\tau_1}\right) + N_2 \frac{1}{\tau_2} \exp\left(-\frac{t}{\tau_2}\right)$$

$$f_1 = \frac{N_1}{N_1 + N_2}$$

tells about the amount of FRET
i.e. Tf binding to TfR

Brief introduction to phasor analysis

Fourier series of a decay $f(t) = \frac{1}{\tau} \exp\left(-\frac{t}{\tau}\right) \longrightarrow f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} g_n \cos\left(2\pi n \frac{t}{T}\right) + s_n \sin\left(2\pi n \frac{t}{T}\right)$

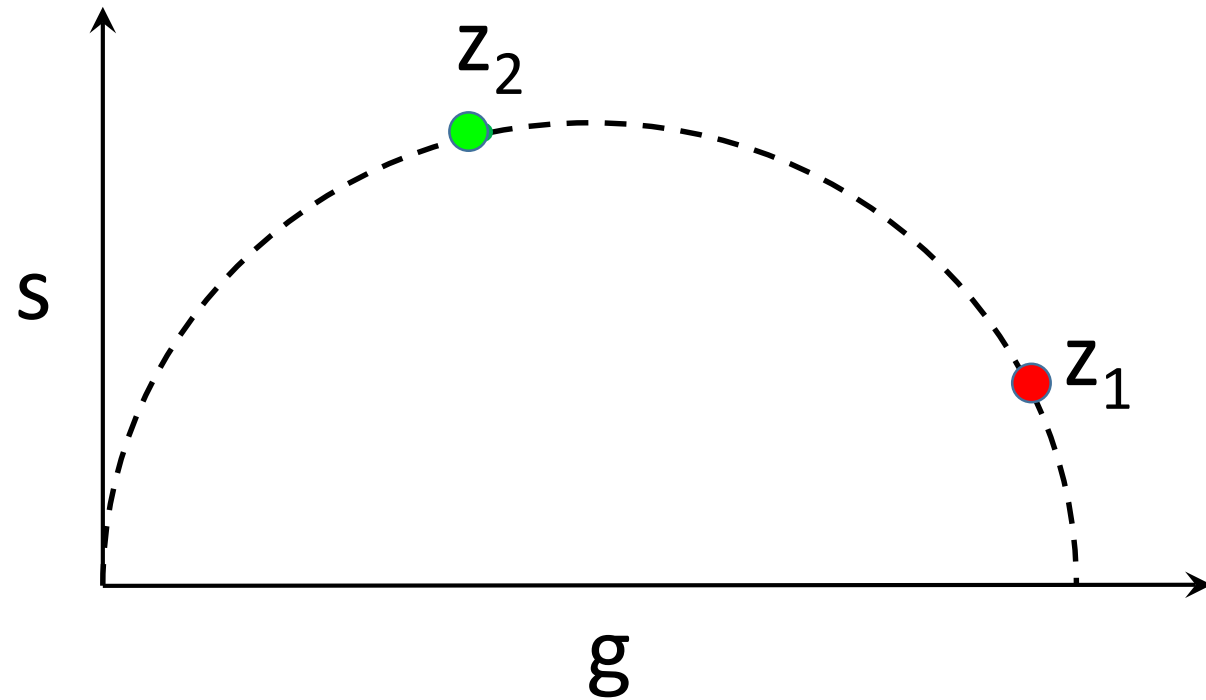
Components of the 1st harmonic: g_1, s_1

$$g_1 = \int_0^T f(t) \cos\left(\frac{2\pi t}{T}\right) dt, \quad s_1 = \int_0^T f(t) \sin\left(\frac{2\pi t}{T}\right) dt$$

$$f(t) = N_1 \frac{1}{\tau_1} \exp\left(-\frac{t}{\tau_1}\right) + N_2 \frac{1}{\tau_2} \exp\left(-\frac{t}{\tau_2}\right)$$

$$\downarrow$$

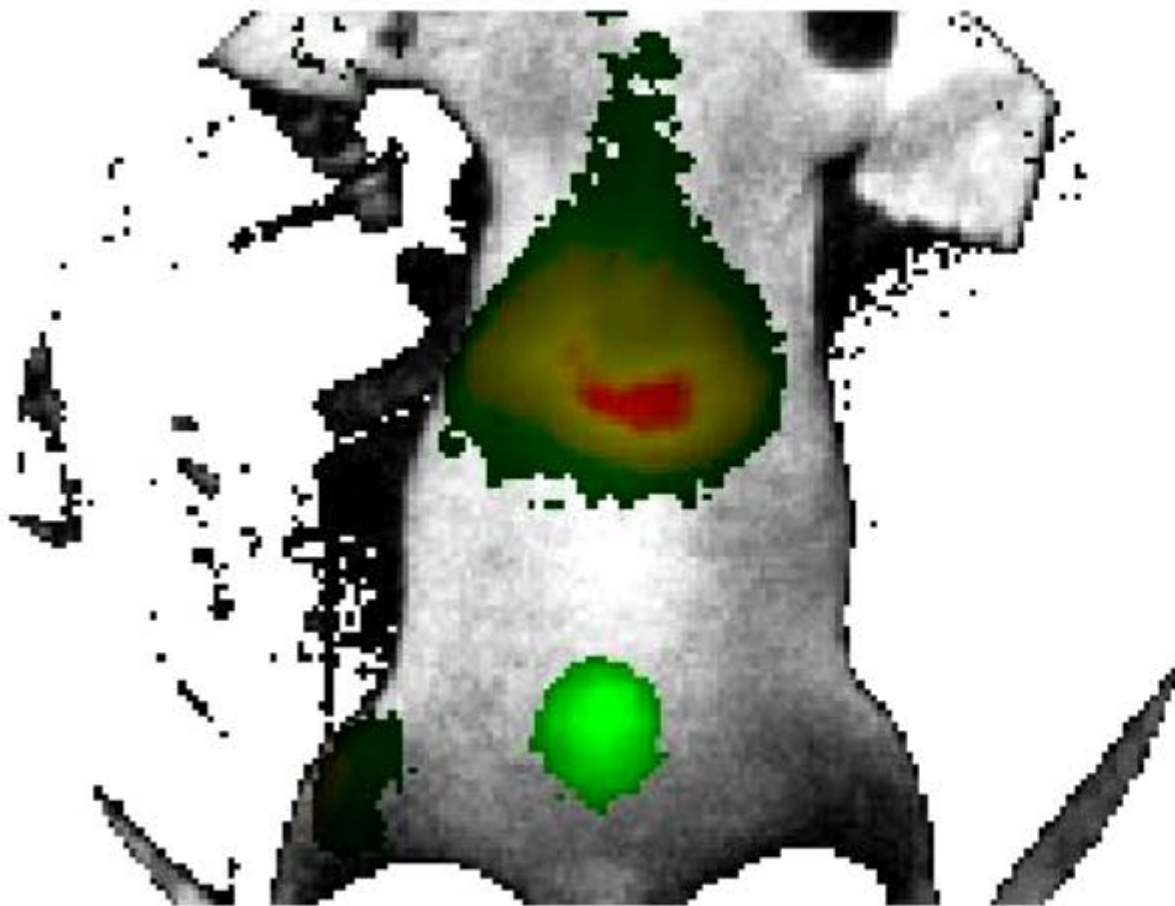
$$f_1 = \frac{N_1}{N_1 + N_2} = \frac{d_1}{d_1 + d_2}$$



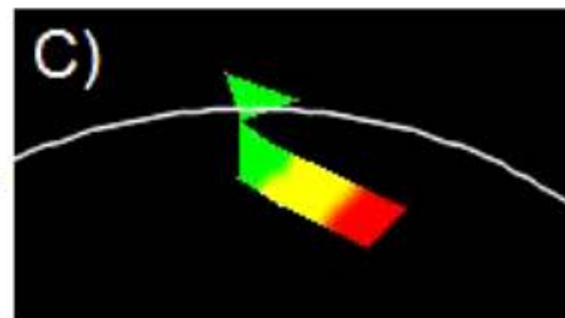
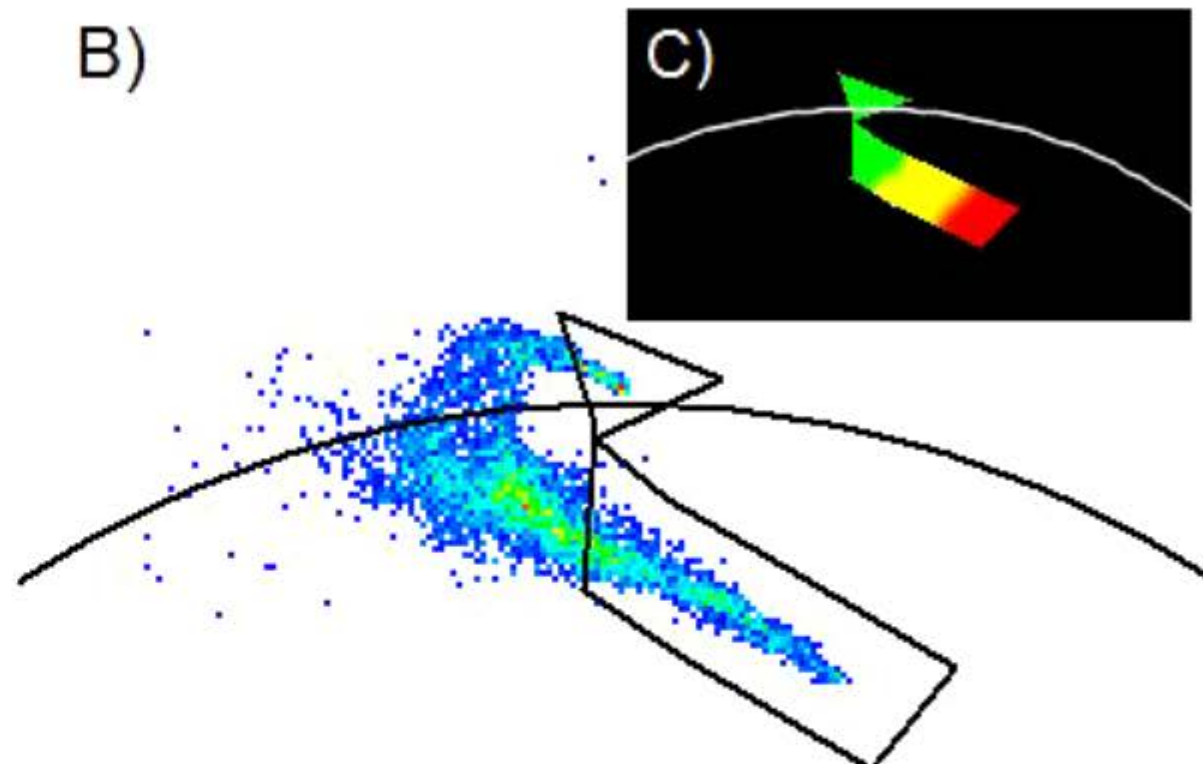
FRET analysis with the phasor approach

A)

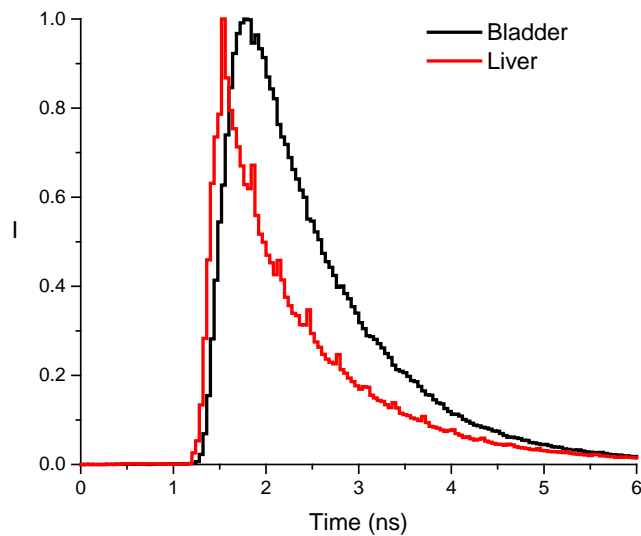
Time point 100



B)

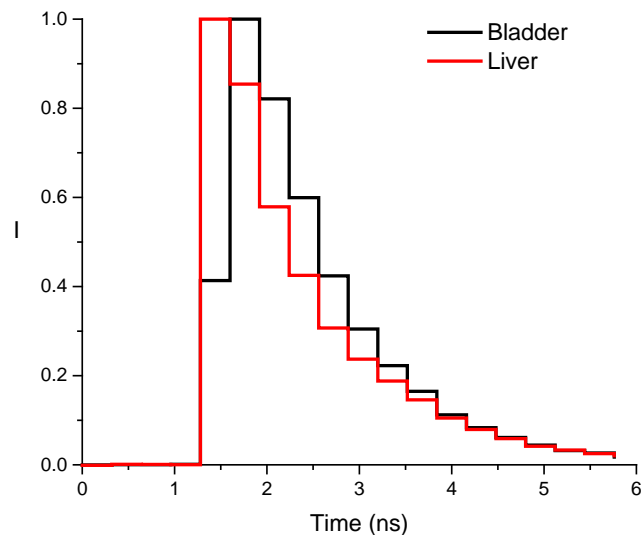


Fewer gates than for decay fitting are needed for quantitative phasor analysis

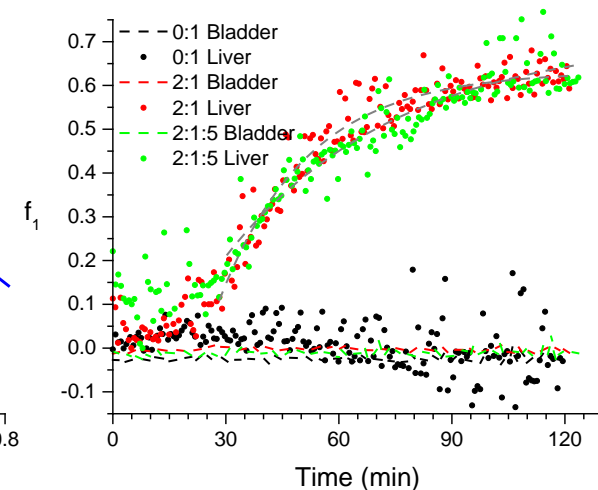
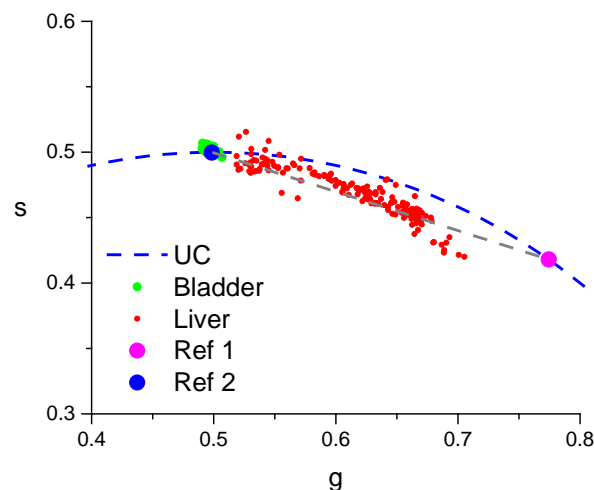
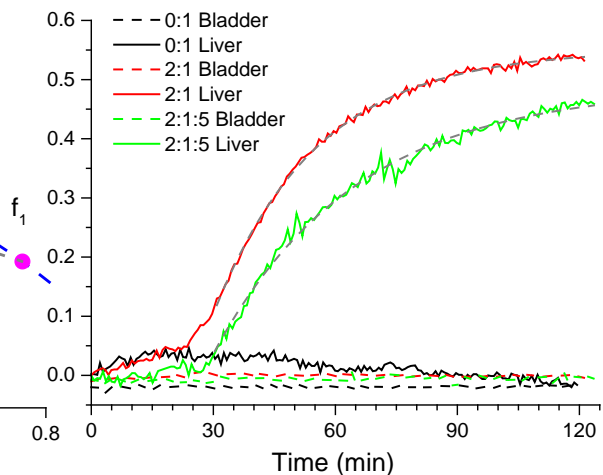
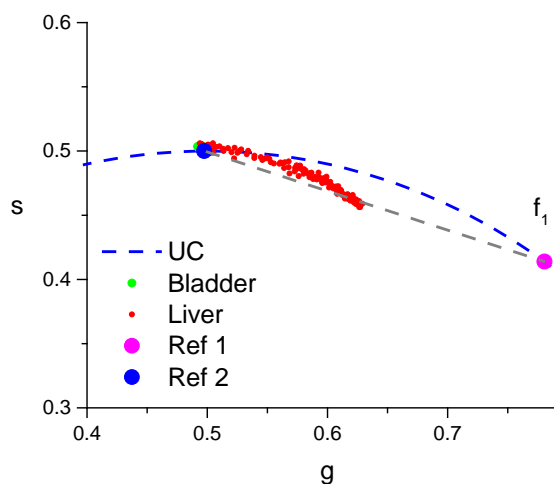


1/8

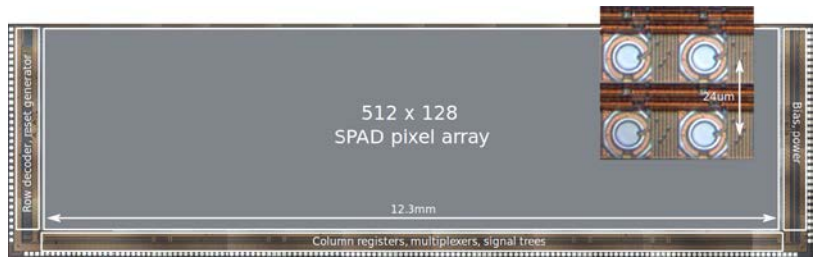
$\tau_{2:1} = 1,528 \pm 15 \text{ s}$
 $\tau_{2:1:5} = 2,109 \pm 55 \text{ s}$



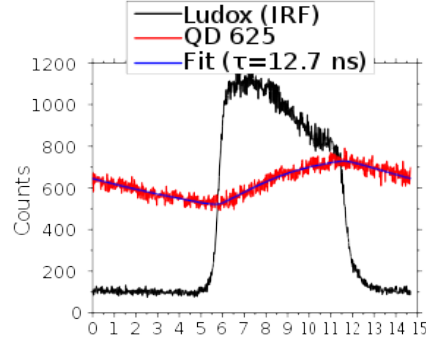
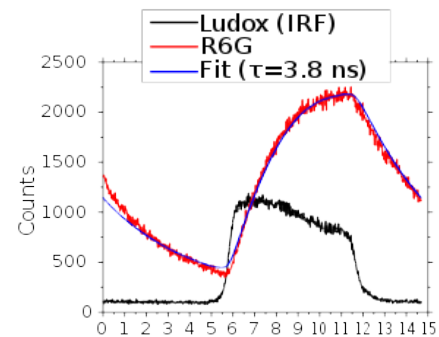
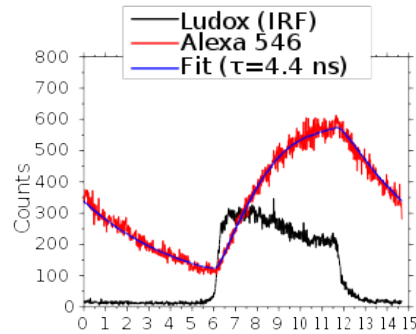
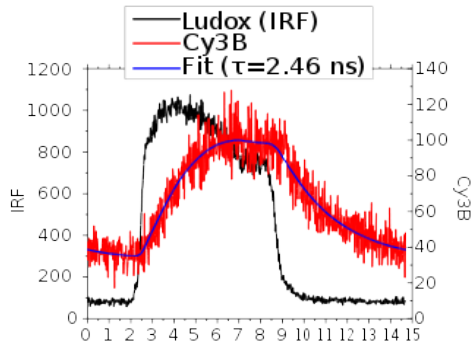
$\tau_{2:1} = 1,418 \pm 93 \text{ s}$
 $\tau_{2:1:5} = 2,769 \pm 356 \text{ s}$



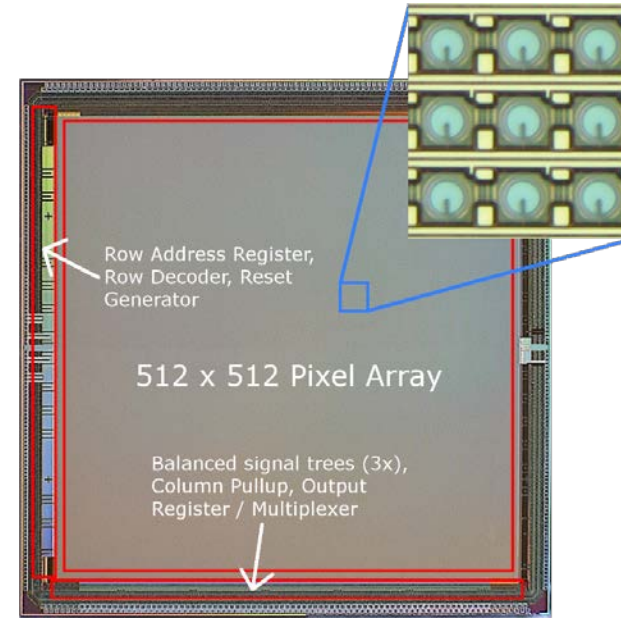
Narrow (or even many) gates are not needed



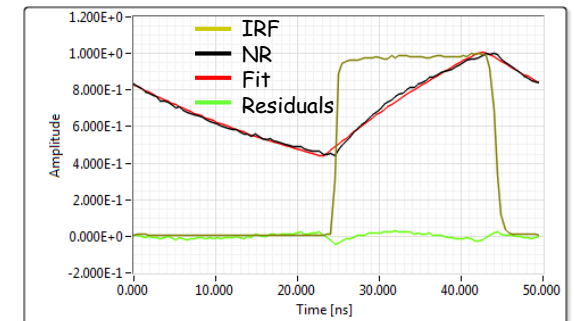
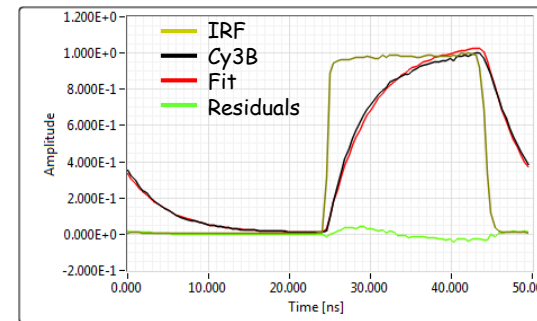
SwissSPAD 1, *Opt. Expr.* 22 (2014)17573



14.7 ns period, 768 gates, 6 ns wide

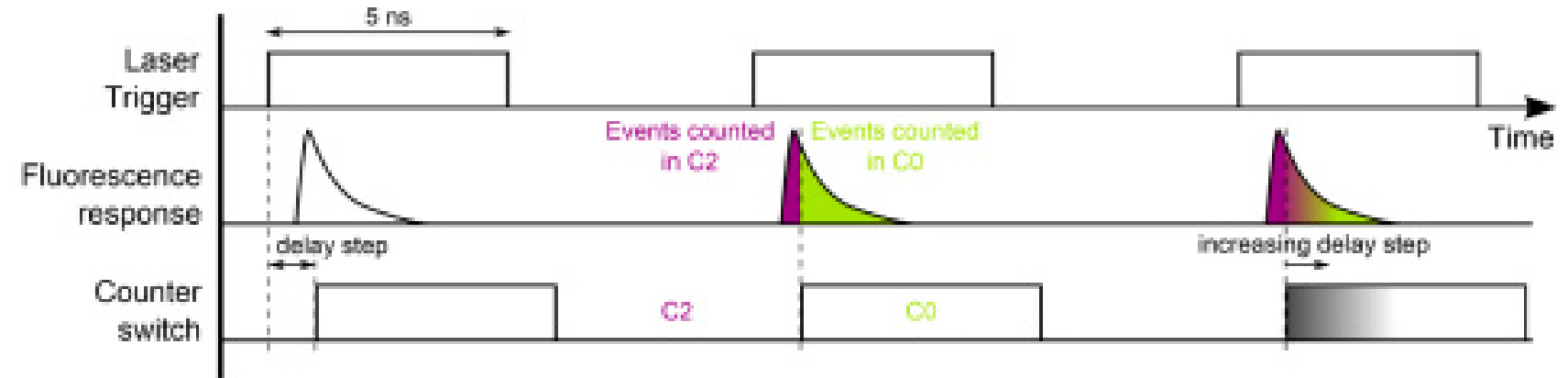
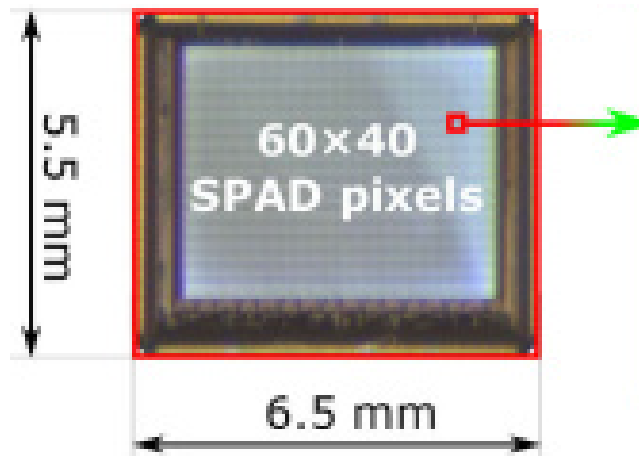


SwissSPAD 2, *IISW* (2017) 234
SPIE BIOS 10498 (2018) 10498-21



50 ns period, 125 gates, 20 ns wide

Pushing the concept of large gates to the limit: FluoCam



Best of both worlds?

- Technical simplicity
- Photon efficiency

FluoCam, *Biomed. Opt. Expr.* **7** (2016) 1797

Conclusion & Perspectives (3)

- Photon-efficient time-resolved counting schemes are worth developing
- TCSPC resolution does not need to be that of LIDAR applications (ps), because measured observables involve 100s-1000s of photons
- *in vivo* NIR (and SWIR) FLI will benefit from improved PDE
- User-modifiable FPGA firmware (or auxiliary NI FPGA?) for data preprocessing (e.g. phasor computation)

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Yung Kuo, Joonhyuck Park, Arkaprabha Basu



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Piera Maccagnani (IMM-CNR, Bologna)
Fabrizio Guerrieri, Federica Villa, Franco Zappa



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Alena Rudkouskaya, Margarida Barroso

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